

## Probabilistic models of the role of oxygen in human decompression sickness

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**Parker, E. C., S. S. Survanshi, P. B. Massell, and P. K. Weathersby.** Probabilistic models of the role of oxygen in human decompression sickness. *J. Appl. Physiol.* 84(3): 1096–1102, 1998.—Probabilistic models of human decompression sickness (DCS) have been successful in describing DCS risk observed across a wide variety of N<sub>2</sub>-O<sub>2</sub> dives but have failed to account for the observed DCS incidence in dives with high PO<sub>2</sub> during decompression. Our most successful previous model, calibrated with 3,322 N<sub>2</sub>-O<sub>2</sub> dives, predicts only 40% of the observed incidence in dives with 100% O<sub>2</sub> breathing during decompression. We added 1,013 O<sub>2</sub> decompression dives to the calibration data. Fitting the prior model to this expanded data set resulted in only a modest improvement in DCS prediction of O<sub>2</sub> data. Therefore, two O<sub>2</sub>-specific modifications were proposed: PO<sub>2</sub>-based alteration of inert gas kinetics (*model 1*) and PO<sub>2</sub> contribution to total inert gas (*model 2*). Both modifications statistically significantly improved the fit, and each predicts 90% of the observed DCS incidence in O<sub>2</sub> dives. The success of *models 1* and *2* in improving prediction of DCS occurrence suggests that elevated PO<sub>2</sub> levels contribute to DCS risk, although less than the equivalent amount of N<sub>2</sub>. Both models allow rational optimization of O<sub>2</sub> use in accelerating decompression procedures.

oxygen effects; gas-exchange kinetics; risk function; hazard function

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PROBABILISTIC MODELS of the risk of human decompression sickness (DCS) have been successful in describing the occurrence and even the time of occurrence of DCS (9, 13, 15, 17, 18). With rare exceptions (14, 19), only inert gases have been considered in such decompression modeling, on the assumption that the role of inert gases in the development of DCS is of overwhelming importance. In nearly all decompression models, inspired O<sub>2</sub> is treated as a “free” quantity and is not linked to the risk of DCS. O<sub>2</sub> is less available as a dissolved gas when it is bound to hemoglobin and when it is converted to the very soluble gas CO<sub>2</sub>. That view is substantiated by measurements of tissue O<sub>2</sub> levels of only a few Torr under normoxic conditions (2).

The most successful probabilistic model has not performed well in predicting DCS risk in dives that use a high fraction (~100%) of O<sub>2</sub> in the breathing gas during decompression (9, 13), underpredicting the occurrence of DCS in these O<sub>2</sub> decompression dives by ~60%. In a subsequent prospective trial of O<sub>2</sub> decompression procedures, severe underprediction again occurred (11).

These results contradicted the expectation of no O<sub>2</sub> effect found in a moderately large study of dives (19) with direct ascent after breathing mixtures with a PO<sub>2</sub> range of 0.2–1.3 atmospheres absolute (ata). The emphasis of the present study is to develop modifications to the previous model to identify a specific O<sub>2</sub> influence on the accumulation of DCS risk. The ideal modification would improve, or not disturb, the model's success with N<sub>2</sub>-O<sub>2</sub> data while better describing the DCS outcomes observed in the O<sub>2</sub> decompression data. Such an improved model could then be applied to the practical optimization of the use of O<sub>2</sub> to accelerate decompression.

The O<sub>2</sub> effects explored here are of two very different forms, both based on observed physiology. In our first model a PO<sub>2</sub>-dependent alteration of the N<sub>2</sub> washin-washout kinetics acknowledges the pharmacological ability of PO<sub>2</sub> to alter central and peripheral circulation. Anderson et al. (1) demonstrated a progressive and significant reduction in cumulative N<sub>2</sub> excretion with increasing inspired O<sub>2</sub>, although the difficult experimental procedure did not allow quantitative estimates of actual N<sub>2</sub> kinetic parameters. In our second model, some of the inspired O<sub>2</sub> is treated as an inert gas, adding to the tissue level of N<sub>2</sub> in leading to DCS risk. Hyperoxia is known to greatly increase PO<sub>2</sub> in tissues (2, 5), and some prior decompression studies concluded that O<sub>2</sub> was approaching N<sub>2</sub> in its DCS risk potency (3, 4, 8, 10). Tikuisis and Nishi (14) explored a bubble-based DCS risk model that included an explicit O<sub>2</sub> contribution, but they did not apply it to data as extensive as those used here, nor did they use it to predict time of DCS occurrence, which is the focus of the present study.

All our models are based on survival functions and are intended to predict the risk of occurrence of an undesirable outcome due to a risk-generating event, in this case the occurrence of DCS after a hyperbaric exposure. We construct a mathematical model that relates a small number of measured variables (time, pressure, gas mix) to a binary outcome (DCS: yes/no). Although we borrow from the terminology of physiology when we use a label such as “partial pressure of gas in tissue,” we have made no direct physiological measurements. Gas terminology is used to aid visualization of a risk function. The success or failure of such a model rests strictly on its ability to predict the probability of occurrence of the outcome.

DATA

The data sets used in fitting models in this report were taken from carefully controlled and well-documented experimental dives conducted in the United States, Canada, and Great Britain, described in detail elsewhere (data sources are described in Ref. 16 with additional sources in Refs. 6 and 11). The basic data set (*group A* in Table 1) used in earlier model development (6, 9) contains 3,322 dives. The data set with ~100% O<sub>2</sub> breathed during decompression (*group B* in Table 1) contains 1,013 dives.

In the *group A* dives, there are 190 DCS and 110 marginal cases, giving an overall DCS incidence of 6.1%. (The APPENDIX lists the data by file names in the primary database of the Naval Medical Research Institute, which is available from the authors.) Marginal cases are mild events considered to be related to the hyperbaric exposure but not severe enough to warrant recompression treatment. These events are given a value of 0.1 DCS case on the basis of the experience of senior diving medical officers (9). Although the majority of dives in *group A* used compressed air (21% O<sub>2</sub>), a large number of dives were performed with moderately enriched O<sub>2</sub> atmospheres. In most of these nonair dives a constant P<sub>O<sub>2</sub></sub> of 0.7 ata was breathed, either throughout the dive or with interspersed periods of air breathing. Other nonair dives used a range of constant fraction of O<sub>2</sub> throughout the dive from 10 to 40%, resulting in P<sub>O<sub>2</sub></sub> of 0.21–1.4 atmospheres absolute (ata) (19). None of the nonair dives used a significantly higher P<sub>O<sub>2</sub></sub> during decompression than during the dive itself. The high P<sub>O<sub>2</sub></sub> values (up to 4.0 ata) in the single-air category come from 58 short-duration (<3 min) dives from a submarine escape experiment, in which high pressures were present for <1 min. Without these 58 profiles, the upper limit of the P<sub>O<sub>2</sub></sub> range for

single-air dives would be 1.5 ata. Only two of the DCS cases in *group A* come from these escape dives.

*Group B* contains 33 DCS and 17 marginal cases, for an incidence of 3.4%. The dives in *group B* are of two types: 1) air dives that use ~100% O<sub>2</sub> during decompression and 2) air dives followed by ~100% O<sub>2</sub> during surface decompression procedures. Surface decompression involves omitting much of the usual decompression requirement, traveling quickly to the surface, and then recompression in a dry hyperbaric chamber, usually to a fixed pressure, after a brief interval at the surface. To allow for incomplete delivery of O<sub>2</sub> to the diver, we assume that immersed divers breathed 99.5% O<sub>2</sub> and dry divers 98% O<sub>2</sub>. The consequences of choosing these particular values are discussed later. P<sub>O<sub>2</sub></sub> within *group B* is 0.21–2.8 ata, with the majority of the O<sub>2</sub> exposures at 1.9 or 2.2 ata, corresponding to decompression stop depths of 30 and 40 feet of seawater.

The data include time of occurrence for all DCS cases and for many of the marginal cases. The time of symptom occurrence is represented in the data as an interval (*T*<sub>1</sub> – *T*<sub>2</sub>) over which symptoms appeared, where *T*<sub>1</sub> is the latest time the diver was known to be entirely free of symptoms and *T*<sub>2</sub> is the time at which definite symptoms were first reported. The methods and rules of establishing *T*<sub>1</sub> – *T*<sub>2</sub> for most reported dives are described in detail elsewhere (16).

MODELS

The best-fitting model from our most recent N<sub>2</sub>-O<sub>2</sub> modeling effort (9, 13) was used as the base model for this study (*model 0*). This model allows for exponential washin and a mixed exponential-linear washout of inert gas partial pressure (9, 12, 13). Risk accumulation for this model is characterized by an instantaneous risk (*r*) proportional to the sum of the risks of each of its three parallel compartments

$$\begin{aligned}
 \text{model 0: } r &= \sum_{i=1}^3 r_i \\
 &= \sum_{i=1}^3 A_i \left( \frac{P_{ti} + P_{met} - P_{amb} - Thr_i}{P_{amb}} \right); \quad (I) \\
 r_i &\geq 0
 \end{aligned}$$

where *A<sub>i</sub>* is a scale factor and P<sub>ti</sub> is the inert (N<sub>2</sub>) gas burden for the *i*th compartment. The inert gas burden represents all inert gas pressure in the compartment, including that in any bubbles present, as though it had remained in solution. P<sub>amb</sub> is the ambient pressure, Thr<sub>*i*</sub> is an estimated threshold parameter (9) for the *i*th compartment, and P<sub>met</sub> is a small constant contribution of metabolic gases (venous P<sub>O<sub>2</sub></sub> and P<sub>CO<sub>2</sub></sub> and water vapor pressure), with a numerical value of 0.19 atmospheres. P<sub>ti</sub> is a function of the arterial inert gas partial pressure (P<sub>aN<sub>2</sub></sub>); a time constant (α<sub>*i*</sub>), which conceptually represents blood perfusion to the tissue; and an estimated linear-exponential kinetic crossover

Table 1. Summary of data

| Type                                 | Dives | Cases |           |      | P <sub>O<sub>2</sub></sub> , ata | F <sub>O<sub>2</sub></sub> |
|--------------------------------------|-------|-------|-----------|------|----------------------------------|----------------------------|
|                                      |       | DCS   | Marginals | %DCS |                                  |                            |
| <i>Group A</i>                       |       |       |           |      |                                  |                            |
| Single air                           | 1,005 | 53    | 13        | 5.4  | 0.21–4.0*                        | 0.21                       |
| Repetitive and multilevel air        | 565   | 34    | 15        | 6.3  | 0.21–1.3                         | 0.21                       |
| Single nonair                        | 678   | 25    | 18        | 4.0  | 0.19–1.5                         | 0.10–0.70                  |
| Repetitive and multilevel nonair     | 607   | 26    | 3         | 4.3  | 0.21–1.2                         | 0.21–0.70                  |
| Saturation                           | 467   | 52    | 61        | 12.4 | 0.21–1.5                         | 0.09–0.21                  |
| <i>Group B</i>                       |       |       |           |      |                                  |                            |
| O <sub>2</sub> decompression         | 586   | 22    | 16        | 4.0  | 0.21–2.8                         | 0.21–0.99                  |
| O <sub>2</sub> surface decompression | 427   | 11    | 1         | 2.6  | 0.21–2.6                         | 0.21–0.98                  |
| Total                                | 4,335 | 223   | 127       | 5.4  |                                  |                            |

DCS, decompression sickness; F<sub>O<sub>2</sub></sub>, fraction of O<sub>2</sub>; ata, atmospheres absolute. Marginal DCS = 0.1 DCS case (8). \*In dives with >1.5 ata P<sub>O<sub>2</sub></sub> in single air category, bottom time was <1 min.

parameter ( $PXO_i$ )

$$\frac{dPti_i}{dt} = \frac{1}{\alpha_i} (Pa_{N_2} - Ps_{N_{2,i}}) \quad (2)$$

where  $Ps_{N_2}$  is the partial pressure of dissolved  $N_2$  in the tissue.

If  $Pti_i \leq (PXO_i + P_{amb} - P_{met})$ , only dissolved gas is present and  $Pti_i$  equals  $Ps_{N_2}$  and gas exchange is simply exponential. If  $Pti_i > (PXO_i + P_{amb} - P_{met})$ , then a bubble is deemed to be present and excess gas comes out of solution, such that the  $Ps_{N_2}$  remains constant at a level of  $(PXO_i + P_{amb} - P_{met})$ . Thus, when depth and  $Pa_{N_2}$  are constant, exchange becomes linear with time. The parameters  $A_i$ ,  $Thr_i$ ,  $PXO_i$ , and  $\alpha_i$  are estimated by fitting to the observed data.

Figure 1 illustrates the handling of inert gas partial pressure in *model 0* for a dive with  $O_2$  decompression. In the hypothetical dive shown, two possible washout curves are plotted: one for a diver who breathes air (solid curve) throughout the decompression and another for a diver who breathes 100%  $O_2$  (dashed curve) during a portion of the decompression. The duration of the  $O_2$  period is indicated by the drop in  $Pa_{N_2}$  below that for breathing air. During the  $O_2$  breathing period,  $N_2$  washout accelerates because  $Pa_{N_2}$ , the asymptote (or forcing function) for the model's calculated  $N_2$  partial pressure ( $Pti_{N_2}$ ), is then essentially zero. Because *model 0* considers DCS risk to be proportional only to the area between the  $Pti_{N_2}$  curve and  $P_{amb}$ , risk is reduced, both in magnitude and duration, because of the  $O_2$  breathing period. This risk reduction agrees qualitatively with the idea that breathing  $O_2$  during decompression reduces the risk of DCS, but comparison of predictions with observed DCS incidence indicates that the reduction is too large (9, 13).

*O<sub>2</sub>-induced kinetic modifications.* The first class of modification (*model 1*) changes the inert gas kinetic time constants for each compartment as a function of

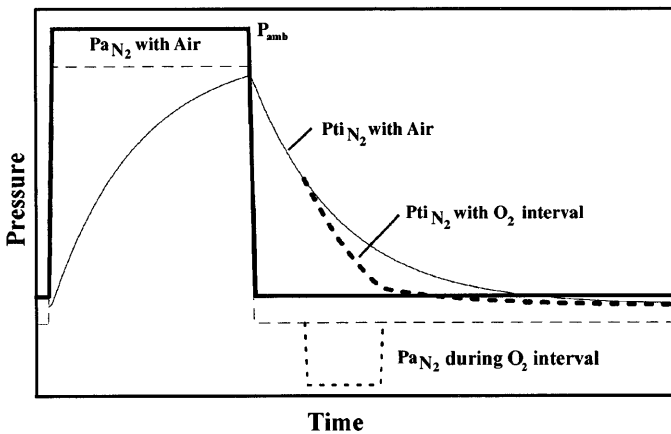


Fig. 1. *Model 0*: preferential washout of  $N_2$  partial pressure in tissue ( $Pti_{N_2}$ ) during  $O_2$  breathing. Dashed line ( $Pa_{N_2}$  with air), arterial pressure of  $N_2$  during air breathing; thin solid curve ( $Pti_{N_2}$  with air), model's washin-washout response; thick dashed line at middle bottom ( $Pa_{N_2}$  during  $O_2$  interval), drop in  $N_2$  pressure during 100%  $O_2$  breathing; thick dashed curve ( $Pti_{N_2}$  during  $O_2$  interval), model's response.

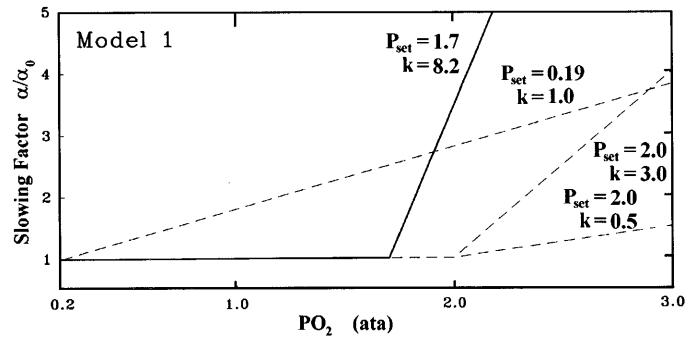


Fig. 2. *Model 1*: possible kinetic slowing effects as a function of  $PO_2$ . Depending on values of estimated parameters  $P_{set}$  and  $k$ , *model 1* may produce a wide range of slowing factors. Solid line, slowing function resulting from best-fitting estimated parameter values.

inspired  $PO_2$ . This type of modification is based on experimental results in which a reduction of whole body  $N_2$  washout was observed with exposure to increasing  $PO_2$  (1). This reduced  $N_2$  washout is attributed to simultaneously observed reductions in cardiovascular parameters, including heart rate and blood flow. These combined effects can be modeled as  $O_2$ -induced reduction of perfusion rate, resulting in increased kinetic time constants. In *model 1* the modified time constant for each compartment is defined as

$$model\ 1: \alpha_i = \alpha_{0,i} [1 + (PO_2 - P_{set}) \cdot k_i]; \quad (3)$$

$$(PO_2 - P_{set}) \geq 0$$

where  $\alpha_{0,i}$  is the unmodified inert gas time constant for the  $i$ th compartment (to be estimated by fitting to data),  $PO_2$  is the inspired  $O_2$  pressure, and  $P_{set}$  and  $k$  are parameters to be estimated from the data.  $P_{set}$  is a pressure threshold above which pressures of  $O_2$  begin to cause kinetic slowing and  $k$  is simply a scale factor necessary to modulate the effect. There is no effect if  $PO_2$  is less than  $P_{set}$ .

Figure 2 shows a range of effects for several values of  $P_{set}$  and  $k$  that *model 1* might have on an  $N_2$  kinetic time constant over the  $PO_2$  range contained in the data. The value on the  $y$ -axis is the exchange retardation factor  $\alpha/\alpha_{0,i}$ . It is clear from Fig. 2 that *model 1* can produce a wide range of subtle-to-pronounced effects, depending on the values of the parameters  $P_{set}$  and  $k$ . In particular, *model 1* is capable of yielding virtually no effect on  $\alpha_0$  for values of  $PO_2$  generally observed in the air dives ( $<1.5$  ata) and an increasing effect for higher  $PO_2$  levels. *Model 1* adds two estimated parameters per kinetic compartment,  $P_{set,i}$  and  $k_i$ , but some of the added parameters may not be warranted statistically and therefore may be dropped.

*O<sub>2</sub> as an inert gas.* In this model,  $O_2$ , at sufficiently high partial pressures, can contribute to bubble formation or growth (3–5, 8, 14). *Model 2* introduces the “ $O_2$  effect” as a direct additive term in the supersaturation part of the risk function. Thus for the inert gas term in Eq. 1

$$model\ 2: Pti_i = Pti_{N_{2,i}} + Pti_{O_{2,i}} \quad (4)$$

These burdens of N<sub>2</sub> and O<sub>2</sub> are governed by their own kinetic time constants. As in *model 0*, exponential and linear kinetics are possible. If  $P_{ti} \leq (P_{amb} + PXO_i - P_{met})$ , then washout is exponential with independent N<sub>2</sub> and O<sub>2</sub> kinetics. However, if  $P_{ti} > (P_{amb} + PXO_i - P_{met})$ , then the N<sub>2</sub> and O<sub>2</sub> washouts become linked, such that the sum of partial pressures of dissolved N<sub>2</sub> and O<sub>2</sub> remains constant at the level of  $(P_{amb} + PXO_i - P_{met})$ .

Not all the O<sub>2</sub> pressure will be considered to be available to contribute to DCS risk. We limit the contribution of O<sub>2</sub> to pressures above a certain level,  $P_{set,i}$ , to be estimated from the data, by controlling the effective O<sub>2</sub> pressure ( $P_{eff,O_2}$ )

$$\begin{aligned} P_{eff,O_2} &= P_{O_2} - P_{set,i}; P_{O_2} > P_{set,i} \\ P_{eff,O_2} &= 0 \quad ; P_{O_2} \leq P_{set,i} \end{aligned} \tag{5}$$

A previous study (14) modeled the effect of O<sub>2</sub> with a similar parameterization, except the parameter  $P_{set}$  was applied asymmetrically. During O<sub>2</sub> uptake both constraints above were followed, whereas during O<sub>2</sub> washout negative values of  $P_{eff,O_2}$  were allowed, which leads to an accelerated washout of O<sub>2</sub>. Under these conditions,  $P_{set}$  is required to simultaneously estimate the level at which O<sub>2</sub> is treated as an inert gas and the degree of enhanced O<sub>2</sub> washout after the dive, two potentially conflicting effects. Our  $P_{set}$  parameter estimates only the level of pressure above which O<sub>2</sub> is treated as an inert gas. *Model 2* adds two estimated parameters per kinetic compartment:  $P_{set,i}$  described above and  $\alpha_{O_2,i}$  the exponential time constant for O<sub>2</sub> washin-washout.

*Model evaluation.* The risk functions, each model's set of equations leading to *Eq. 1*, were cast in standard risk (or hazard) function form to predict the probability of each observed dive in the data set and then into a likelihood (or log likelihood, LL) function. Details, especially those required to properly account for time of DCS onset, have been presented previously (17). Parameter estimation, propagation of errors, and formulation of likelihood ratio (LR) tests used standard methods, as in prior work (9, 15, 17, 18).

Each of the O<sub>2</sub> effect models is a modification of, and can be simplified to, *model 0*; therefore, an LR test (7, 18) is used to test for the significance of the added parameters contained in each modification. A proposed model will have a significantly improved fit to the data (at  $P = 0.5$ ) if its LL exceeds the *model 0* LL (smaller negative number) by at least 1.92 for one added parameter and 2.98 for two added parameters, out to 6.30 for six added parameters (7). Each model was fitted to the combined data set (*A + B*). *Models 1* and *2* allow for up to six new parameters (2 per kinetic compartment) to be estimated, in addition to the kinetic time constants, scale factors, thresholds, and linear-exponential crossover parameters, which are common to all. Some or all of the added parameters may not add significantly to the improvement of the fit, as judged by the LR test. Final results for each model were chosen among many

parameter estimation runs to include only those parameters the existence of which was justified at  $P < 0.05$ .

*Results of fitting.* Ideally, the O<sub>2</sub> effect parameters of any model would describe the data from *group B* in Table 1 and allow the basic parameters (those relating to *Eq. 1*) to better describe the data in *group A*. Table 2 lists the best-fit parameters and SEs estimated for each model.

The best fit of *model 1* improved LL by 11.1 units with only two additional estimated parameters, applied to *compartment 2*. The improvement is significant at  $P < 0.01$ . In *model 1*, estimated O<sub>2</sub> effect parameters result in no alteration of the N<sub>2</sub>-based kinetics for  $<1.7$  ata inspired  $P_{O_2}$ . A rapidly increasing effect was produced for higher values of  $P_{O_2}$ , up to an exchange retardation factor of  $\sim 10$  (10 times slower gas kinetics) at 2.8 ata, the upper limit of  $P_{O_2}$  in the *group B* dives. The *model 1* effect curve for these estimated parameter values is shown in Fig. 2 (solid line). Additional O<sub>2</sub> effect parameters for *compartments 1* and *3* did not significantly improve LL.

The best fit of *model 2* improved the LL fit by 10.5 with two additional estimated parameters applied to *compartment 2*. This improvement is also significant at  $P < 0.01$ . The estimated N<sub>2</sub> time constant is substantially longer (slower) for *model 2* in *compartment 2* than for *model 0*. Although this slower time constant will result in less uptake of inert gas, it will also slow washout, thus allowing for longer risk accumulation for many dives. The specific O<sub>2</sub> effect parameters for this

Table 2. Estimated parameters for models fitted to data *A + B*

| Parameter      | Compartment        |                    |                    | LL      |
|----------------|--------------------|--------------------|--------------------|---------|
|                | 1                  | 2                  | 3                  |         |
| <i>Model 0</i> |                    |                    |                    |         |
| $\alpha$       | 1.50 ± 0.71        | 32.5 ± 14.4        | 407.1 ± 19.0       | 1,200.1 |
| <i>A</i>       | 3.6E-3<br>(2.7E-3) | 4.5E-5<br>(2.1E-5) | 1.0E-3<br>(1.2E-4) |         |
| PXO<br>Thr     |                    | 0.0 ± 0.03         | 0.02 ± 0.01        |         |
| <i>Model 1</i> |                    |                    |                    |         |
| $\alpha$       | 1.61 ± 0.77        | 57.6 ± 16.0        | 508.4 ± 32.6       | 1,189.0 |
| <i>A</i>       | 3.2E-3<br>(2.4E-3) | 1.2E-4<br>(3.6E-5) | 1.1E-3<br>(1.5E-4) |         |
| PXO<br>Thr     |                    | 0.03 ± 0.02        | 0.07 ± 0.02        |         |
| $P_{set}$      |                    | 1.69 ± 0.09        |                    |         |
| <i>k</i>       |                    | 8.23 ± 5.68        |                    |         |
| <i>Model 2</i> |                    |                    |                    |         |
| $\alpha$       | 1.42 ± 0.75        | 85.8 ± 19.0        | 516.6 ± 43.9       | 1,189.6 |
| <i>A</i>       | 3.4E-3<br>(2.7E-3) | 1.8E-4<br>(5.1E-5) | 9.4E-4<br>(1.4E-4) |         |
| PXO<br>Thr     |                    | 0.06 ± 0.02        | 0.07 ± 0.02        |         |
| $P_{set}$      |                    | 1.03 ± 0.23        |                    |         |
| $\alpha_{O_2}$ |                    | 82.5 ± 67.8        |                    |         |

Values are estimated parameters ± SE; LL, log likelihood;  $\alpha$ , nitrogen time constant (min); *A* and *k*, scale factors (dimensionless); PXO, linear-exponential kinetic crossover parameter (ata); Thr, threshold parameter (ata);  $P_{set}$ , O<sub>2</sub> pressure threshold (ata);  $\alpha_{O_2}$ , oxygen time constant (min).

Table 3. Prediction of DCS occurrence for models fit to data A + B

| Type                                 | Observed DCS Cases | Predicted DCS Cases |             |             |             |
|--------------------------------------|--------------------|---------------------|-------------|-------------|-------------|
|                                      |                    | Model 0             | Model 1     | Model 2     | Model 0A    |
| <i>Group A</i>                       |                    |                     |             |             |             |
| Single air                           | 54.3               | 48.8 ± 7.2          | 45.8 ± 7.2  | 45.9 ± 7.5  | 44.5 ± 7.4  |
| Repetitive and multilevel air        | 35.5               | 43.9 ± 5.9          | 40.7 ± 5.9  | 40.6 ± 6.3  | 39.9 ± 6.1  |
| Single nonair                        | 26.8               | 28.8 ± 4.3          | 26.4 ± 4.4  | 27.9 ± 4.2  | 25.7 ± 4.5  |
| Repetitive and multilevel nonair     | 26.3               | 38.2 ± 5.0          | 32.0 ± 5.3  | 32.0 ± 7.6  | 31.1 ± 5.7  |
| Saturation                           | 58.1               | 52.8 ± 10.8         | 61.3 ± 13.9 | 60.1 ± 14.0 | 61.4 ± 14.1 |
| Total                                | 201.0              | 212 ± 27            | 206 ± 27    | 207 ± 27    | 203 ± 27    |
| <i>Group B</i>                       |                    |                     |             |             |             |
| O <sub>2</sub> decompression         | 23.6               | 17.9 ± 3.4          | 19.4 ± 4.4  | 19.5 ± 4.6  | 9.9 ± 3.4   |
| O <sub>2</sub> surface decompression | 11.1               | 8.1 ± 2.0           | 12.2 ± 4.0  | 13.5 ± 4.7  | 3.8 ± 1.3   |
| Total                                | 34.7               | 26.0 ± 5.2          | 31.5 ± 8.1  | 31.2 ± 9.7  | 13.7 ± 4.4  |
| Total                                | 235.7              | 238 ± 30            | 237 ± 32    | 237 ± 30    | 216 ± 30    |

Values are model predictions ± 95% confidence level.

model apply a direct risk addition to *compartment 2* through the “combined”  $Pt_i$  (Eq. 4). This O<sub>2</sub>-based contribution replaces overpressure “lost” due to the slower N<sub>2</sub> washin and applies this added risk specifically to the high-PO<sub>2</sub> segments only (PO<sub>2</sub> > P<sub>set</sub> = 1.03 ata).

#### PREDICTION OF DCS

Table 3 lists the DCS occurrence predicted by each of the candidate models for the data used in fitting, along with the 95% confidence limits of each prediction obtained from propagation of errors. The last column in Table 3 gives predictions from *model 0* fit to *group A* only (*model 0A*). As expected, *model 0* predicts DCS in the combined data better than *model 0A* just by calibration to the combined A + B data. For example, the total DCS predicted by *model 0* increased to 238, from 216 predicted by *model 0A*, compared with 236 observed cases. This improvement is accomplished by increased prediction of DCS for all data types except saturation dives. However, *model 0* continues to underpredict DCS incidence in *group B* (by 25.1%) and fails to include the observed value within the 95% confidence limits of its prediction in *group B*, either as a whole or in its subsets.

It is clear from Table 3 that *models 1* and *2* have most of the desired predictive ability: prediction of DCS occurrence in *group A* dives centered nearly on the observed value and prediction of DCS occurrence in *group B*, which includes the observed value within its confidence limits. Also, *models 1* and *2* have maintained the quality of prediction of *model 0A* for dives in *group A*.

Tables similar to Table 3 can be used in  $\chi^2$  tests of “goodness of fit,” where large values of the test statistic are taken as “failure” of the model to describe the distribution of the data. We can test each model’s ability to predict DCS within each data group by separately considering the five categories of *group A* and two of *group B* from Table 3. The resulting *model 0*, *1*, and *2* test statistics are 6.6, 2.9, and 3.3 for *group A* [4 degrees of freedom (df)] and 2.9, 1.0, and 1.3 for *group B*

(1 df), respectively. None of these models “fails” to fit: all these  $\chi^2$  values yield  $P > 0.05$ . Similarly, we can break the 26 categories in the APPENDIX into the 21 belonging to *group A* and the 5 belonging to *group B*. The resulting *model 0*, *1*, and *2* test statistics are 23.3, 19.7, and 20.0 for *group A* and 11.8, 6.6, and 6.7 for *group B*. All *group A* tests yield  $P > 0.05$  for 20 df. For *group B*, *model 0* has  $P < 0.05$  and *models 1* and *2* have  $P > 0.05$  for 4 df. This data categorization provides an indication that *model 0* does not predict DCS occurrence in the dives of *group B* as well as *models 1* and *2*. However, the outcomes of such  $\chi^2$  tests are clearly dependent on the choice of categorization. From results such as these and from many other instances where arbitrary but “reasonable” recategorization of data leads to “large”  $\chi^2$  statistics, we believe that such tests are only useful as a rough guide to identify problem areas. These areas can be identified more readily using line-by-line comparisons of observed and predicted results.

The inclusion of time of occurrence in our data allowed us to compare the predictive performance of the candidate models with the observed time distribution of DCS incidence. Figure 3 shows the observed and

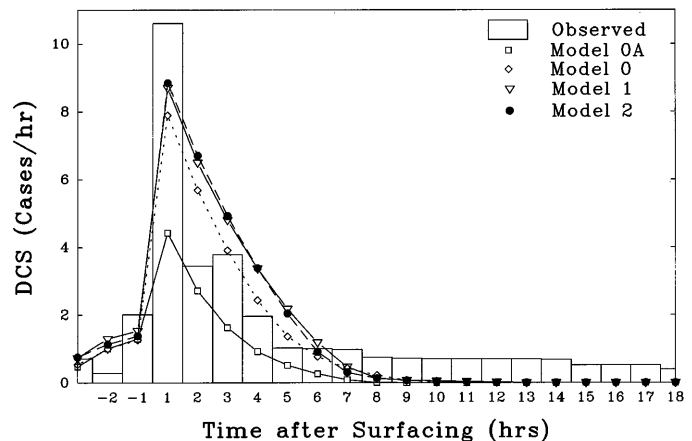


Fig. 3. Time of occurrence of decompression sickness (DCS). Predicted and observed DCS cases are shown for each hour after diver surfaces.

predicted DCS cases in each 1-h interval after surfacing for the dives in *group B*. Negative times indicate relatively rare events occurring during decompression before the divers reach the surface. *Model 0A* clearly underpredicts occurrence as a function of time throughout. *Model 0* shows substantial improvement over *model 0A*, with increased prediction for at least 8 h after the divers surface. *Models 1* and *2* have nearly identical predictions of occurrence in all time intervals but tend to overpredict in the 2- to 5-h range. Because almost one-third of the DCS cases are observed within the 1st h after surfacing, a good prediction here is particularly important. Here, the prediction of *model 2* (8.9 cases/h) comes closest to matching this value observed in the 1st h (10.6) but differs only slightly from that of *model 1* (8.7).

## DISCUSSION

Both models of an O<sub>2</sub> contribution to DCS successfully described the expanded data set. Are the fully parameterized models plausible in light of the supposed underlying physiology? Because *model 1* was intended to incorporate the experimental observations of Anderson et al. (1), we compared the behavior of this model with those observations. They reported 9 and 17% reductions in the volume of whole body N<sub>2</sub> elimination compared with normoxic levels over 2 h of washout at 2.0 and 2.5 ata PO<sub>2</sub>, respectively. By use of the best-fit parameters shown in Table 2, the time constant for N<sub>2</sub> elimination in the second of three compartments in *model 1* was increased by factors of 2.55 and 6.67 at 2.0 and 2.5 ata PO<sub>2</sub>, respectively. A decrease in blood flow of >80% is large but not inconceivable. Over a 2-h washout period, these increased calculated time constants would result in 60 and 85% reductions, respectively, of the N<sub>2</sub> elimination expected from the unmodified time constant of 57.6 min, taking into account the asymmetric washout due to the mixed linear-exponential kinetics. It is reasonable to ignore the very fast and very slow compartments of the model compared with the experiment of Anderson et al. If *compartment 2* represents ~15–20% of the total N<sub>2</sub> gas volume, then the calculated reductions in N<sub>2</sub> elimination would translate approximately into the reported 9 and 17% whole body reductions.

Another human decompression study attempted to analyze N<sub>2</sub> exchange retardation from high O<sub>2</sub> pressures (19). Over the experimental range of 0.2–1.3 ata PO<sub>2</sub>, the single N<sub>2</sub> time constant did not appear to change, but parameter uncertainty allows the ~90-min time constant to slow to as much as ~130 min, which would represent an 18% reduction in N<sub>2</sub> elimination over a 2-h washout period.

*Model 2* represents an approach fundamentally different from *model 1*, in that O<sub>2</sub>, when present in pressures greater than P<sub>set<sub>i</sub></sub> (Table 2), contributes directly to the risk generating overpressure, as defined in *Eqs. 1* and *4*. The estimated value of 1.03 ata for P<sub>set<sub>2</sub></sub> requires that no O<sub>2</sub> effect on DCS risk be seen at pressures lower than this. This is a plausible threshold, in that O<sub>2</sub> levels in the tissue can be kept low until the hemoglobin dissocia-

tion curve is fully saturated above ~1.0 ata. A P<sub>set</sub> of 1.03 ata allows for a contribution to DCS risk accumulation of 25–60% of the O<sub>2</sub> present during decompression in the dives of *group B*. This result is in general agreement with some animal studies (3, 4, 8, 10), which called for a 25–33% contribution from O<sub>2</sub>. A prior human study (19) did not require an O<sub>2</sub> effect on risk but placed an upper bound of 40% contribution up to 1.3 ata PO<sub>2</sub> and thus is consistent with the present result. We note that combinations of *models 1* and *2*, incorporating a kinetic slowing and a direct contribution effect, were not successful in improving the fit relative to *model 1* or *model 2* as fit separately.

Our O<sub>2</sub> effect modifications were intended to remedy the failure of *model 0* to account for the DCS incidence observed in the O<sub>2</sub> data. Because our data coding of the inspired O<sub>2</sub> level in this data set is critical in all models, we should ask whether our data misrepresented the diver's actual gas exposure. In particular, we have explored the possibility that the coding of dry chamber O<sub>2</sub> decompressions, which form the bulk of *group B*, at 98% O<sub>2</sub> is incorrect because of imperfect delivery of the gas. Estimates from experienced investigators suggest that the minimum O<sub>2</sub> fraction likely to be present in the face mask in dry exposures is ~85–95% (R. Y. Nishi, personal communication). If the actual O<sub>2</sub> exposures were much less than our indicated 98%, *model 0*, without a specific O<sub>2</sub> contribution to DCS risk, might be able to account for the DCS incidence observation in *group B*. To explore this, *model 0* was calibrated to a series of altered data sets, with these dry O<sub>2</sub> exposures in *group B* modified to 60–90%. Only at ≤70% O<sub>2</sub> was *model 0* able to accurately predict the DCS outcome in *groups A* and *B*. With the data coded at ≥80%, the model's predictions were minimally changed from those shown for *model 0* in Table 3 (first "predicted" column). Thus our coding of the data at 98% does not directly "create" the need for an O<sub>2</sub> effect; even at a conservative value of 85%, *model 0* fails to describe the O<sub>2</sub> data. Similarly, inward skin flux of ambient N<sub>2</sub> from the air-filled chamber would increase the total body N<sub>2</sub> content but is unlikely to correspond to 20–30% of air breathing.

A third O<sub>2</sub> effect model added a fourth parallel risk compartment to *Eq. 1*, in which risk accumulation was based solely on PO<sub>2</sub> rather than on PN<sub>2</sub>. The best fit of this model improved the LL by only 3.8 (LL = 1196.3) with two additional estimated parameters: a time constant and a scale factor. Although this was a statistically significant improvement, it was not as impressive as those of *models 1* and *2*. This model's prediction of DCS incidence in *group A* was similar to that of *model 0*, and its prediction of DCS in *group B* (29.5 ± 6.9), although an improvement, was again less impressive than that of *model 1* or *model 2*. Its relatively poor fit and its problematic tie to plausible physiology led us to abandon the model.

The present results suggest that use of O<sub>2</sub> much over 1 ata has drawbacks that warrant consideration in optimizing decompression. This does not mean that O<sub>2</sub>

is not useful during decompression, only that O<sub>2</sub> is not totally free of concern for causing DCS. Either of the two new models can be used for O<sub>2</sub> decompression optimization.

## APPENDIX

### Individual data set observed and predicted DCS cases

|                                      | Observed DCS | Predicted DCS |         |         |          |
|--------------------------------------|--------------|---------------|---------|---------|----------|
|                                      |              | Model 0       | Model 1 | Model 2 | Model 0A |
| <i>Group A</i>                       |              |               |         |         |          |
| Single air                           |              |               |         |         |          |
| EDU885A                              | 30.0         | 28.2          | 27.5    | 27.7    | 26.6     |
| DC4W                                 | 8.4          | 5.7           | 5.7     | 5.5     | 5.6      |
| SUBX87                               | 2.0          | 0.6           | 0.5     | 0.5     | 0.5      |
| NMRNSW                               | 5.5          | 6.1           | 5.3     | 5.6     | 5.2      |
| PASA                                 | 5.2          | 3.4           | 2.8     | 2.6     | 2.7      |
| NSM6HR                               | 3.2          | 4.9           | 4.0     | 4.1     | 3.9      |
| Repetitive and multi-level air       |              |               |         |         |          |
| EDU885AR                             | 11.0         | 11.7          | 12.0    | 11.8    | 11.7     |
| DC4WR                                | 3.0          | 1.0           | 1.0     | 1.0     | 0.9      |
| PARA                                 | 7.3          | 10.5          | 9.8     | 9.6     | 9.6      |
| PAMLA                                | 14.2         | 20.6          | 18.1    | 18.3    | 17.6     |
| Single nonair                        |              |               |         |         |          |
| NMR8697                              | 12.8         | 17.0          | 15.4    | 16.4    | 15.1     |
| EDU885M                              | 4.0          | 3.8           | 3.5     | 3.5     | 3.4      |
| EDU1180S                             | 10.0         | 7.9           | 7.5     | 8.1     | 7.3      |
| Repetitive and multi-level nonair    |              |               |         |         |          |
| EDU184                               | 11.0         | 15.6          | 14.3    | 14.7    | 13.9     |
| PAMLAOD                              | 6.0          | 9.8           | 7.6     | 7.1     | 7.3      |
| PAMLAOS                              | 5.3          | 7.9           | 6.1     | 6.0     | 5.9      |
| EDU885S                              | 4.0          | 4.9           | 4.1     | 4.2     | 3.9      |
| Saturation                           |              |               |         |         |          |
| ASATEDU                              | 15.7         | 12.9          | 15.0    | 14.4    | 15.0     |
| ASATNMR                              | 1.0          | 4.6           | 4.6     | 4.1     | 4.5      |
| ASATNSM                              | 20.1         | 17.8          | 22.5    | 22.6    | 22.7     |
| ASATARE                              | 21.3         | 17.5          | 19.2    | 18.9    | 19.2     |
| <i>Group B</i>                       |              |               |         |         |          |
| O <sub>2</sub> decompression         |              |               |         |         |          |
| DC8AOW                               | 3.1          | 0.7           | 0.9     | 1.0     | 0.4      |
| DC8AOD                               | 3.2          | 3.5           | 3.2     | 4.5     | 1.6      |
| NMR94EOD                             | 17.3         | 13.7          | 15.2    | 14.0    | 7.9      |
| O <sub>2</sub> surface decompression |              |               |         |         |          |
| DC8ASUR                              | 10.1         | 6.3           | 9.8     | 9.1     | 2.9      |
| DCSUREP                              | 1.0          | 1.8           | 2.5     | 2.6     | 0.9      |

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