Research Article

Na Wang, Yuan Du*, Qingtao Gong*, Ning Liu, and Yao Teng

Research on the low-frequency multiline spectrum vibration control of offshore platforms

https://doi.org/10.1515/rams-2021-0075 received August 10, 2021; accepted October 02, 2021 **Keywords:** offshore platform, typical structure, low-frequency multiline spectrum, dynamic vibration absorption

Abstract: With the increasing scale, complexity and diversity of supporting equipment of offshore platform, the low-frequency vibration of equipment such as dynamic positioning system and the main engine is difficult to attenuate in the propagation process of the platform structure, which causes a local resonance of platform, aggravates the fatigue damage of structure and causes discomfort to the human body. Dynamic vibration absorption is widely used in the low-frequency vibration control of offshore platforms; however, there is little research about the multiline spectrum vibration control method in the local resonance region of platforms. In the current research, we first take the stiffened plate under multipoint excitation as the research object, and the effectiveness of the optimal homology design method of dynamic vibration absorption is verified. Subsequently, the low-frequency multiline spectrum vibration control method about the local resonance region of the offshore platform is proposed. Finally, a large offshore platform is chosen as the research object and the measured load of the main engine is taken as the input to calculate the vibration response of the platform. The effect of distributed dynamic vibration absorption of the resonance area verifies the effectiveness of the vibration control method presented in the article and provides a basis for the engineering application.

College, Ludong University, Yantai 264025, People's Republic of China, e-mail: gqt2008@163.com **Na Wang:** College of Power and Energy Engineering, Harbin Engineering University, Harbin, 150001, People's Republic of China **Ning Liu:** College of Shipbuilding Engineering, Harbin Engineering University, Harbin, 150001, People's Republic of China

Yao Teng: College of Power and Energy Engineering, Harbin Engineering University, Harbin, 150001, People's Republic of China; CIMC Raffles Offshore Ltd., Yantai 264000, People's Republic of China

1 Introduction

In the background of global economic development, offshore platform plays an increasingly important role in the exploration and exploitation of offshore oil and gas resources. Meanwhile, with the increasing scale and complexity of the offshore platform and supporting equipment, the structural vibration of the offshore platform caused by equipment cannot be ignored [1–3]. The familiar vibration control methods of offshore platforms can be divided into three types: passive control, semi-active control [4] and active control [5,6]. Passive control relies on the interaction between the device and the main structure, which does not need the input of external energy. In addition, passive control has the advantage of simple structure, good economy and stable performance [7]. For this reason, it has been widely used in marine engineering.

The common passive control forms include vibration isolation, energy dissipation and vibration absorption [2]. Vibration isolation is achieved by installing vibration isolation devices between the main structure and the vibration source. Common vibration isolation methods for offshore platforms can be divided into two categories: foundation vibration isolation and structural vibration isolation [8]. Foundation vibration isolation is realized by adding vibration isolation and energy dissipation devices between the bottom of the platform deck and the jacket [9]. The structural vibration isolation is implemented by changing the local structure of the platform. For example, the support leg of the offshore platform is divided into the vibration sharing structure composed of inner and outer pipes. Numerous experimental and calculation results have shown that the vibration isolation device can effectively reduce the vibration of the offshore platform [8,10,11]. However, vibration isolation measures are usually applicable to newly constructed platforms. It is neither convenient nor economical to adopt vibration isolation measures for completed platforms.

3 Open Access. © 2022 Na Wang *et al.*, published by De Gruyter. **(C)** BY This work is licensed under the Creative Commons Attribution 4.0 International License.

 ^{*} Corresponding author: Yuan Du, College of Power and Energy Engineering, Harbin Engineering University, Harbin, 150001, People's Republic of China, e-mail: duyuan@hrbeu.edu.cn
 * Corresponding author: Qingtao Gong, Ulsan Ship and Ocean

In the method of energy dissipation, the vibration of the main structure is consumed in the deformation and reciprocating movement of energy dissipation dampers. The common energy dissipation dampers for offshore platforms can be divided into two types: velocity- and displacement-dependent dampers. Displacement-dependent dampers include friction dampers and metal yield dampers. The energy dissipation of displacement-dependent dampers [12,13] is related to displacement and has nothing to do with the structural velocity response and frequency, so it is suitable for low-frequency vibration of platforms [14]. Shape memory alloy (SMA) is a classical kind of displacement-dependent damper.

As a novel type of smart materials, SMAs exhibit unique properties such as shape memory effect (SME), corrosion resistance, fatigue resistance and high reliability [15,16]. SME was first recognized by Buehler and Wang in the alloy of nickel and titanium, which withstands large deformation of up to 10 percent with no residual strain. The SME of smart materials makes it a terrific candidate for energy dissipation appliances and dampers [17]. In the recent studies of SMAs, Choi et al. [18] researched the impacts of geometric parameters on recovering aptitude of SMA fibers, and test samples with different diameters and crimped lengths have been investigated in detail. To better understand the tribological behavior of SMAs, Levintant-Zayonts et al. [19] conducted the ball-on-plate reciprocating sliding wear tests on NiTi SMAs under different test working conditions. Dutta and Majumder [20] applied Nitinol (an alloy of Ni and Ti) SMA damper to control the vibration of structures affected by the underground blast. A steel structure with various arrangements of the dampers was analyzed and compared with conventional steel bracing. Kamarian et al. [21] compared the thermal bucking behavior of simply supported composite beams composed of SMAs and carbon nanotubes. Dynamic mechanical thermal analysis and thermomechanical analysis experiments were also conducted on the above materials. Sheikhi et al. [22] studied the static and dynamic behavior of rubber bearing composed of SMA and structural steel (SS). By means of the finite element method, the thickness ratio between SMA and SS on different dampers has also been investigated in different bridge models. Li et al. [23-27] proposed a new semi-analytical method to analyze the vibration behavior of typical structures composed of laminated materials and functionally graded materials.

However, energy dissipation usually requires large relative deformation and the relative deformation of damping devices in the offshore platform is not always large enough, which results in a poor damping effect. To improve the vibration control effect of SMAs in offshore platforms, Ghasemi et al. [28] combined the advantage of SMA and tuned mass damper (TMD) to control the vibration of offshore platforms by means of simplifying the platform and the dynamic vibration absorption as a multi-degree of freedom system; the effects of SMA TMD under broadband frequency excitations have been discussed in detail.

The dynamic vibration absorption is not limited by the relative deformation of the main structure and it has been a wide concern to scholars and engineers. By means of arranging the dynamic vibration absorption subsystem on the main structure and adjusting the parameters of the subsystem, the vibration of the main structure is absorbed through the movement of the dynamic vibration absorption subsystem.

At present, tuned liquid damper (TLD) [29,30] and TMD [28,31-34] are the two main dynamic vibration absorption forms used in offshore platforms. TLD is a subsystem attached to the main structure that contains liquid. When the TLD moves with the main structure, the sloshing and viscous motion of liquid in the container will dissipate the energy of the main structure and reduce the vibration. Vandiver and Mitome [35] proposed the application of TLD to the vibration control of the offshore platform in 1979, and the vibration characteristics of the platform after placement of TLD were analyzed. Finally, the vibration reduction effect of TLD was verified. Lee et al. [36] studied the vibration reduction effect of TLD on a typical tension leg floating platform. Through numerical simulation and experiments, it is verified that the tuned TLD system can effectively reduce the dynamic response of the offshore platform. Jin et al. [37] studied the influence of TLD on the vibration response of the platform under seismic waves, and the corresponding numerical analysis was conducted through the lumped mass method and compared with the model test results subsequently. The comparison results showed that the centralized mass method can effectively simulate the effect of TLD on the platform vibration control, and the frequency and mass ratio of TLD are the main influential factors of the vibration control effect. Lotfollahi et al. [38] also analyzed the control effect of TLD on the platform vibration under seismic wave excitation, and the parameters of TLD were optimized based on the finite element analysis results.

TMD can be simplified as a subsystem composed of mass, damping and spring. Many scholars have studied the theory and the application of TMD in offshore platform vibration control. Yue et al. [39] carried out many field tests on the Bohai Bay oil platform. The test results showed that when the ice sheet passes through the pile legs of the jacket platform, the main frequency of ice-induced load excitation is close to the natural frequency of the platform, which leads to ice-induced vibration of the platform. The calculation results showed that the ice-induced vibration of the platform can be effectively reduced by placing TMD. Taflanidis et al. [40] designed TMD for the tension leg platform under random wave load based on the simulation results, and an excellent vibration absorption effect is achieved in two different directions. Chandrasekaran et al. [41] also took the tension leg platform under random wave load as the research object, and the vibration control effects of single TMD and multiple TMD were compared.

In a word, many researchers have carried out research in the application of dynamic vibration absorption on offshore platforms and achieved a number of results. Whereas most research is limited to single-order global vibration of offshore platforms, a few studies have been conducted on the vibration control of local resonance region and low-frequency multiline spectrum dynamic vibration absorption of offshore platforms.

In view of the above shortcomings, we are inspired by the following literature studies [42–45] to solve this problem. The main innovations of the current research can be summarized as follows: First, the low-frequency multiline spectrum vibration control method of offshore platforms is put forward in the current research. By arranging distributed dynamic vibration absorption, the multiline spectrum vibration of the platform can be controlled simultaneously. Second, the modal superposition method is combined with the low-frequency multiline spectrum vibration control method. Through the establishment of an equivalent numerical model of the local resonance region, the efficiency of the dynamic vibration absorption design is greatly improved. Finally, the effectiveness of the current method is verified by the calculation of a largescale offshore platform, which lays the foundation for engineering applications.

2 Theoretical basis

When the main structure is simplified as a single degree of freedom system, the schematic diagram of the main structure with dynamic vibration absorber can be described as in Figure 1. As displayed in Figure 1, the mass, stiffness and damping of the main structure are, respectively, m_1 , c_1 and k_1 . Meanwhile, the mass, stiffness and damping of the dynamic vibration absorber correspond to m_2 , c_2 and k_2 , respectively. When the force acting on the main structure is $F_1e^{i\omega t}$, the displacements of the main system and dynamic



Figure 1: Schematic diagram of the dynamic vibration absorber with the main structure.

vibration absorber are x_1 and x_2 , and the coordinate origin is located at static equilibrium positions, respectively.

According to Newton's second law, the general form of the differential equation of the dynamic vibration absorber and the main structure can be expressed as follows [5,32]:

$$\begin{bmatrix} m_1 & 0 \\ 0 & m_2 \end{bmatrix} \begin{pmatrix} \ddot{x}_1 \\ \ddot{x}_2 \end{pmatrix} + \begin{bmatrix} c_1 + c_2 & -c_2 \\ -c_2 & c_2 \end{bmatrix} \begin{pmatrix} \dot{x}_1 \\ \dot{x}_2 \end{pmatrix}$$

$$+ \begin{bmatrix} k_1 + k_2 & -k_2 \\ -k_2 & k_2 \end{bmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} F_1 e^{i\omega t} \\ 0 \end{pmatrix}.$$
(1)

The special solutions of equation (1) can be set as follows:

$$\begin{cases} x_1 \\ x_2 \end{cases} = \begin{cases} X_1 \\ X_2 \end{cases} e^{i\omega t}.$$
 (2)

Further solution of the steady-state response amplitude of the main structure is expressed as follows:

$$X_{1} = \frac{F_{1}}{k_{1}} \times \left\{ \frac{(\nu^{2} - \eta^{2}) + i(2\zeta\eta\nu)}{\eta^{4} - (1 + \nu^{2} + \mu\nu^{2})\eta^{2} + \nu^{2} + i(2\zeta\eta\nu)[1 - (1 + \mu)\eta^{2}]} \right\}$$
(3)

In the above equation (3), v is the frequency ratio between the dynamic vibration absorber and the main structure, η is the frequency ratio between the external load and the main structure and μ is the mass ratio:

$$\boldsymbol{\nu} = \sqrt{\frac{k_2}{m_2}} \sqrt{\frac{m_1}{k_1}}, \qquad (4)$$

$$\eta = \frac{\omega}{\sqrt{k_{\rm l}/m_{\rm l}}},\tag{5}$$

$$\mu = \frac{m_2}{m_1},\tag{6}$$

In addition, ζ is the damping ratio of the dynamic vibration absorber, which is the ratio between damping of TMD and critical damping:



Figure 2: Schematic diagram of loading points and assessment nodes of the plate frame structure: (a) loading point and (b) assessment points.

$$\boldsymbol{\zeta} = \boldsymbol{c}_2/\boldsymbol{c}_c, \tag{7}$$

$$c_c = 2\sqrt{m_2 k_2}.$$
 (8)

In equations (7) and (8), c_c is the critical damping, m_2 and k_2 are, respectively, mass and stiffness of the dynamic vibration absorber. Den Hartog [46] derived the closed formulas of the optimal frequency ratio and damping parameters and expressed as follows:

$$\nu = \frac{\omega_n}{\Omega_n} = \frac{1}{1+\mu},\tag{9}$$

$$\zeta_{\rm opt} = \sqrt{\frac{3\mu}{8(1+\mu)^3}} \,. \tag{10}$$

3 Numerical simulation and discussion

3.1 Dynamic vibration absorption design of grillage under multipoint excitation

As displayed in Figure 2, the length and width of the stiffened plate are, respectively, a = 5 and b = 5 m and the thickness of the stiffened plate is h = 0.025 m. Meanwhile, the width, height and length of the rib are, respectively, $b_b = 0.05$ m, $h_b = 0.1$ m and L = 5 m. The ribs are, respectively, located at y = 1.5 m and y = 3.5 m. The density of the material of the stiffened plate is $\rho = 7,850$ kg \cdot m⁻³, and the Poisson's ratio and Young's modulus are, respectively, $\mu = 0.3$ and $E = 2.1 \times 10^{11}$ Pa.

The loading points displayed in Figure 2(a) are, respectively, geometric center (2.5,2.5) and (2.5,3.5) of the stiffened plate, and the assessment points are displayed in Figure 2(b).

The first three natural frequencies of the stiffened plate under clamped boundary conditions are shown in Table 1.

Under the action of a unit force at the loading points shown in Figure 2(a), the vibration displacement curve of assessment points in Figure 2(b) is shown in Figure 3.

It can be seen from Figure 3 that the peak corresponds to 19.8 Hz (the third-order natural frequency) does not appear in the frequency–response curve of assessment point 1. Analysis suggests that the reason is point 1 is located at the node of the third-order vibration mode. Compared with assessment point 1, the new peak generates at the third-order natural frequency of 19.8 Hz in the vibration curve of assessment point 2. The vibration–response curve of assessment point 3 and 4 is almost the same as assessment point 2.

As displayed in Figure 3, the maximum and secondorder resonance peaks of typical assessment points, respectively, appear at the first-order 9.3 Hz and the third-order 19.8 Hz. Therefore, the first- and third-order modes of the stiffened plate will be chosen as the control object in the subsequent design of the low-frequency multiline spectrum distributed by the dynamic vibration absorption device.

Table 1: Natural frequencies of the grillage structure (Hz)

Modal order	First	Second	Third
Grillage	9.3	17.4	19.8



Figure 3: Frequency–response curves of typical assessment points: (a) assessment point 1 (2.5,2.5), (b) assessment point 2 (2.5,1.5), (c) assessment point 3 (2.5,3.5) and (d) assessment point 4 (1.6,4.2).

First, the equivalent modal mass [46] to be controlled at the position of the dynamic vibration absorption of the stiffened plate is solved by equation (11):

$$M_{ik} = \frac{\Delta m_{ik} \omega_{ik}^2}{\Omega_i^2 - \omega_{ik}^2} \Omega_i.$$
(11)

In equation (11), M_{ik} represents the equivalent mass of point *k* in the *i*th order, Δm_{ik} represents the additional given mass at the layout position *k* of the dynamic vibration absorption, Ω_i represents the *i*th natural frequency (rad·s⁻¹) of the stiffened plate, and ω_{ik} is the *i*th natural frequency (rad·s⁻¹) of the coupling system after the stiffened plate is attached with the given mass.

According to the calculation, the corresponding equivalent mass at the antinode of the first-order mode of the stiffened plate is 898.8 kg, and the corresponding equivalent mass at the antinode of the third-order mode is 988.2 kg. The optimal frequency ratio and damping parameters are, respectively displayed, in equations (9) and (10). When the mass ratio is set as 0.02, the parameters of the dynamic vibration absorption can be obtained by referring to the above formula.

The dynamic vibration absorption devices are set as the parameters in Table 2 and installed at the antinode of the first- and third-order vibration mode of the stiffened plate, respectively. The layout position of dynamic vibration absorption and the schematic diagram of assessment points are separately shown in Figure 4(a) and (b):

The comparison of vibration–response curves of typical assessment points in Figure 4(b) before and after the installation of dynamic vibration absorber are demonstrated in Figure 5.

Parametert	Mass ratio	Mass (kg)	Spring stiffness $(N \cdot m^{-1})$	Damping coefficient $(N \cdot s \cdot m^{-1})$
First order	0.02	18.0	61557.4	180.4
Third order	0.02	19.8	294662.4	413.9

Table 2: Parameter table of dynamic vibration absorbers for plate structures

The Figure 5 displays the comparison of frequency-response curves of typical points based on the optimal homology design method. When the mass ratio of the dynamic vibration absorption device is set to 0.02, the first- and third-order resonance peak of each assessment point decreases more than 27 and 25 dB, which verifies the effective control of the low-frequency multiline spectrum of the stiffened plate. In addition, the vibration absorption effect decreases with the increase of the distance between the assessment point and the installation position of the dynamic vibration absorption.

3.2 Low-frequency multi-line spectrum vibration control method of offshore platforms

In the previous section, we analyzed the distributed dynamic vibration absorption of the stiffened plate under multipoint excitation. On the basis of this, the research on the low-frequency multiline spectrum vibration control method of platforms will be carried out in this section. The control process is shown in Figure 6.

It can be seen from Figure 6 that the low-frequency multiline spectrum vibration control method of the offshore platform mainly includes the following parts: (1) Establishment of an equivalent numerical model of the local resonance area to be controlled. (2) The solution of equivalent mass and parameters of dynamic vibration absorption device. (3) Verification of dynamic vibration absorption effect. The specific process is given in the following sections.

3.2.1 Equivalent numerical model of the local resonance area

By means of combining the finite element cloud diagram and frequency–response curve of the assessment points, the local resonance region can be determined. Then, the free vibration of the local resonance region can be calculated. Finally, the boundary conditions of the equivalent numerical model of the local resonance region can be determined by comparing with the frequency–response curve.

3.2.2 Parameter design of the dynamic vibration absorber

Based on the vibration mode of the equivalent numerical model of the local resonance area, the vicinity of the



Figure 4: Schematic diagram of assessment points and the placement position of the dynamic vibration absorption of the plate frame structure: (a) placement position of the dynamic vibration absorber and (b) location of the assessment point.



Figure 5: Comparison of frequency–response curves of typical assessment points: (a) assessment point 1 (2.5,2.5), (b) assessment point 2 (2.5,1.5), (c) assessment point 3 (2.5,3.5), and (d) assessment point 4 (1.6,4.2).

antinode of the mode to be controlled is selected as the installation position of the dynamic vibration absorption device. Further, the equivalent mass of the mode to be controlled at the installation position of the dynamic vibration absorption is determined based on formula (11). In addition, the parameters of the dynamic vibration absorption device are determined by combining the optimal homology equations (9) and (10).

3.2.3 Verification and analysis of the vibration absorption effect

Finally, the effect of the dynamic vibration absorption device is verified on the basis of the finite element method.

3.3 Verification of the low-frequency multiline spectral vibration control of the offshore platform

A large offshore platform is chosen as the research object in this section, and the low-frequency multiline spectrum vibration of the local resonance area of the offshore platform has been controlled on the basis of the research mentioned above.

3.3.1 Dynamic analysis model and the load of the platform

As a complex structure, when analyzing its dynamic characteristics, it is necessary to reasonably simplify



Figure 6: Low-frequency multiline spectrum vibration control process of the offshore platform.



Figure 7: Main engine load of the semi-submersible support platform.

the offshore platform, equipment and flow field. In addition, it is necessary to select the appropriate size of the mesh to divide the model. During the meshing process, the longitudinal and transverse spacings of the grid shall not be greater than the strong frame spacing and longitudinal truss spacing, respectively. Taking into account the solution accuracy and efficiency, the finite element scale is finally determined to be 0.5 m. The final finite element model of the platform includes 340,904 surface elements and 140,900 beam elements.

Six main engines are arranged on the platform, with a power of 4,950 kW. The speed of the main engine is 720 rpm and the weight of each main engine is 84 t. The vibration acceleration of the main engine tested on the ship is displayed in Figure 7, which is applied vertically



Figure 8: Vibration response of the superstructure cab: (a) 12 Hz and (b) 19 Hz.



Figure 9: Vibration–response curves of typical nodes of the superstructure cab: (a) assessment point #7, (b) assessment point #8, (c) assessment point #9 and (d) assessment point #10.

to the mass point above the base corresponding to the main engines.

3.3.2 Platform vibration response

Based on the finite element model superposition method, the vibration response of the platform is analyzed. The partial response cloud plot of the superstructure cab at frequencies of 12 and 19 Hz are, respectively, shown in Figure 8(a) and (b). It is clear that the vibration response cloud of the superstructure cab at frequencies of 12 and 19 Hz are, respectively, well consistent with the first- and fourth-order vibration mode of the local resonance area.

The assessment points of #7–#10 displayed in Figure 8 are chosen as the typical assessment points, and the vibration–response curves of the assessment points are displayed in Figure 9.

Table 3: Equivalent mass of the cab truncation model and parameters of dynamic vibration absorption devices

Parameter	Mass ratio	Mass (kg)	Spring stiffness $(N \cdot m^{-1})$	Damping coefficient (N·s·m ⁻¹)
First order	0.02	147.0	819126.1	1891.0
Fourth order	0.02	80.5	1125242.3	1640.6



Figure 10: Comparison of the cloud chart of the vibration acceleration response before and after distributed dynamic vibration absorption of the cab deck. (a) Comparison of nephograms before and after dynamic vibration absorption layout of 12 Hz. (b) Comparison of nephograms before and after dynamic vibration absorption layout of 19 Hz.

Assessment points #7 and #8 are both located near the antinode of the first-order vibration mode of the superstructure cab. The response of assessment points #7 at 12 Hz is greater than 19 Hz, and the response of assessment points #8 at 12 Hz and 19 Hz is similar. In addition, assessment points #9 and #10 are located near the antinode of the vibration mode corresponding to 19 Hz. Therefore, the response of the above assessment points #9 and #10 at 19 Hz is slightly greater than 12 Hz. It follows that the amplitude of the vibration–response curve of the assessment point is determined by the location of assessment points and load characteristics.

3.3.3 Dynamic vibration absorption design in the local resonance region

According to the flow in Figure 6, the low-frequency multiline spectrum vibration control of the superstructure cab has been conducted. Depending on the vibration response nephogram of the superstructure cab and the bulkhead partition, the local resonance region is partitioned. When the boundary condition is set as simply supported, the vibration modes of the local resonance region at corresponding frequencies are basically consistent with the overall finite element calculation results of the platform.

The antinodes of 12 and 19 Hz modal shapes in the local resonance area of the superstructure cab are, respectively, selected as the installation position of the dynamic vibration absorption. According to equation (11), the equivalent mass of the 12 and 19 Hz mode antinodes are 7348.5 and 4026.7 kg, respectively. When the mass ratio is set as 0.02, the parameters of dynamic vibration absorption are as listed in Table 3.

When the dynamic vibration absorption devices are arranged at antinodes of 12 and 19 Hz modes, respectively. The cloud diagram of the vibration response before and after the dynamic vibration absorber is arranged as shown in Figure 10:

It is easy to find that under the combined action of the distributed dynamic vibration absorber, the vibration response of the driving deck at 12 and 19 Hz is significantly reduced. Meanwhile, the corresponding comparison of vibration acceleration response curves of typical assessment points is listed in Figure 11.



Figure 11: Vibration response of typical nodes of the superstructure cab before and after optimization of typical examination points of the upper cab: (a) assessment point #7, (b) assessment point #8, (c) assessment point #9 and (d) assessment point #10.

To sum up, by combining the low-frequency multiline spectrum vibration control method of the platform with the finite element method, the low-frequency multiline spectrum vibration of the local resonance region of the platform is effectively controlled. The vibration acceleration of typical assessment points at 12 and 19 Hz decreased by more than 13 dB.

4 Conclusion

In the current research, by means of combining the lowfrequency multiline spectrum vibration control process and modal superposition method, the low-frequency multiline spectrum distributed dynamic vibration absorption method of the platform is proposed. First, the current research status of the vibration control methods of offshore platforms is briefly introduced. Then, we give a brief introduction to the theoretical basis of dynamic vibration absorption. Afterward, a stiffened plate under clamped boundary conditions is chosen as the research object to investigate the effect of distributed dynamic vibration absorption devices. Finally, the lowfrequency multiline spectrum vibration control process of the offshore platform is proposed. The effectiveness of the proposed method is also verified in the calculation of the platform. The conclusions of the current research are as follows:

- The amplitude of the vibration–response curve of the assessment point is determined by the location of the assessment point and load characteristics.
- (2) When the dynamic vibration absorption mass ratio is set as 0.02, the vibration acceleration response curve

at signature frequencies (12 and 19 Hz) decreases by more than 13 dB under the action of distributed dynamic vibration absorption.

(3) By means of combining the low-frequency multiline spectrum vibration control method with the finite element method, the multiline spectrum vibration in the local resonance region of the offshore platform is controlled effectively and quickly.

Acknowledgements: I would like to express my gratitude to all editors who helped me during the writing of this thesis.

Funding information: This study was funded by the National Natural Science Foundation of China (52101351, U2006229), the National Key Research and Development Program (2016YFC0303406), and the Key Research and Development Program of Shandong Province (2019JZZY010125, 2020CXGC-010701, 2020CXGC010702).

Author contributions: Yuan Du, Qingtao Gong contributed to the conception of the study. Na Wang, Ning Liu, Yao Teng performed the data analyses and wrote the manuscript.

Conflict of interest: The authors declare that they have no conflict of interest.

Data availability statement: The data used to support the findings of this study are included within the article.

References

- Asiri, S. A. and Y. Z. AL-Zahrani. Theoretical analysis of mechanical vibration for offshore platform structures. *World Journal of Mechanics*, Vol. 4, No. 1, 2014, pp. 1–11.
- [2] Zhang, B.-L., Q.-L. Han, and X.-M. Zhang. Recent advances in vibration control of offshore platforms. *Nonlinear Dynamics*, Vol. 89, No. 2, 2017, pp. 755–771.
- [3] Liu, Y., Z. Lu, X. Yan, Z. Liu, and L. Tang. Measurement and modelling of the vibration induced by working equipment on an offshore platform. *Ocean Engineering*, Vol. 219, 2021, id. 108354.
- [4] Som, A. and D. Das. Seismic vibration control of offshore jacket platforms using decentralized sliding mode algorithm. *Ocean Engineering*, Vol. 152, 2018, pp. 377–390.
- [5] Kandasamy, R., F. Cui, N. Townsend, C. C. Foo, J. Guo, A. Shenoi, et al. A review of vibration control methods for marine offshore structures. *Ocean Engineering*, Vol. 127, 2016, pp. 279–297.

- [6] Zhang, B., Q. Han, X. Zhang, and G. Tang. *Active control of offshore steel jacket platforms*, Springer, Singapore, 2019.
- [7] Sarkar, S. and B. Fitzgerald. Vibration control of spar-type floating offshore wind turbine towers using a tuned massdamper-inerter. *Structural Control and Health Monitoring*, Vol. 27, No. 1, 2020, id. e2471.
- [8] Xu, Z.-D., F.-H. Xu, and X. Chen. Vibration suppression on a platform by using vibration isolation and mitigation devices. *Nonlinear Dynamics*, Vol. 83, No. 3, 2016, pp. 1341–1353.
- [9] Wang, S., Q. Yue, and D. Zhang. Ice-induced non-structure vibration reduction of jacket platforms with isolation cone system. *Ocean Engineering*, Vol. 70, 2013, pp. 118–123.
- [10] Xu, Z. D., X. H. Huang, F. H. Xu, and J. Yuan. Parameters optimization of vibration isolation and mitigation system for precision platforms using non-dominated sorting genetic algorithm. *Mechanical Systems and Signal Processing*, Vol. 128, 2019, pp. 191–201.
- [11] Ma, R., K. Bi, and H. Hao. Heave motion mitigation of semisubmersible platform using inerter-based vibration isolation system (IVIS). *Engineering Structures*, Vol. 219, 2020, id. 110833.
- [12] Golafshani, A. A. and A. Gholizad. Friction damper for vibration control in offshore steel jacket platforms. *Journal of Constructional Steel Research*, Vol. 65, No. 1, 2009, pp. 180–187.
- [13] Patil, K. and R. Jangid. Passive control of offshore jacket platforms. *Ocean Engineering*, Vol. 32, No. 16, 2005, pp. 1933–1949.
- [14] Minh Le, L., D. Van Nguyen, S. Chang, D. Kim, S. G. Cho, and D. D. Nguyen. Vibration control of jacket offshore wind turbine subjected to earthquake excitations by using friction damper. *Journal of Structural Integrity and Maintenance*, Vol. 4, No. 1, 2019, pp. 1–5.
- [15] Enferadi, M. H., M. R. Ghasemi, and N. Shabakhty. Waveinduced vibration control of offshore jacket platforms through SMA dampers. *Applied Ocean Research*, Vol. 90, 2019, id. 101848.
- [16] Zhang, X., B. H. Tan, and Z. Li. Seismic performance and iceinduced vibration control of offshore platform structures based on the ISO-PFD-SMA brace system. *Advances in Materials Science and Engineering*, Vol. 92, 2017, pp. 1061–1074.
- [17] Sellitto, A. and A. Riccio. Overview and future advanced engineering applications for morphing surfaces by shape memory alloy materials. *Materials*, Vol. 12, No. 5, 2019, id. 708.
- [18] Choi, E., B. Mohammadzadeh, J. H. Hwang, and J. H. Lee. Displacement-recovery-capacity of superelastic SMA fibers reinforced cementitious materials. *Smart Structures and Systems*, Vol. 24, No. 2, 2019, pp. 157–171.
- [19] Levintant-Zayonts, N., G. Starzynski, M. Kopec, and S. Kucharski. Characterization of NiTi SMA in its unusual behaviour in wear tests. *Tribology International*, Vol. 137, 2019, pp. 313–323.
- [20] Dutta, S. C. and R. Majumder. Shape memory alloy (SMA) as a potential damper in structural vibration control. Advances in Manufacturing Engineering and Materials, Springer, Cham, 2019, 485–492.
- [21] Kamarian, S., M. Bodaghi, R. B. Isfahani, and J. Song. A comparison between the effects of shape memory alloys and carbon nanotubes on the thermal buckling of laminated

composite beams. *Mechanics Based Design of Structures and Machines*, 2020, pp. 1–24. Doi: 10.1080/ 15397734.2020.1776131.

- [22] Sheikhi, J., M. Fathi, R. Rahnavard, and R. Napolitano. Numerical analysis of natural rubber bearing equipped with steel and shape memory alloys dampers. *Structures*, Elsevier, Vol. 32, 2021, pp. 1839–1855.
- [23] Li, H., F. Pang, X. Wang, Y. Du, and H. Chen. Free vibration analysis for composite laminated doubly-curved shells of revolution by a semi analytical method. *Composite Structures*, Vol. 201, 2018, pp. 86–111.
- [24] Li, H., F. Pang, H. Chen, and Y. Du. Vibration analysis of functionally graded porous cylindrical shell with arbitrary boundary restraints by using a semi analytical method. *Composites, Part B: Engineering*, Vol. 164, 2019, pp. 249–264.
- [25] Li, H., F. Pang, Q. Gong, and Y. Teng. Free vibration analysis of axisymmetric functionally graded doubly-curved shells with un-uniform thickness distribution based on Ritz method. *Composite Structures*, Vol. 225, 2019, id. 111145.
- [26] Li, H., F. Pang, Y. Li, and C. Gao. Application of first-order shear deformation theory for the vibration analysis of functionally graded doubly-curved shells of revolution. *Composite Structures*, Vol. 212, 2019, pp. 22–42.
- [27] Li, H., F. Pang, X. Miao, S. Gao, and F. Liu. A semi analytical method for free vibration analysis of composite laminated cylindrical and spherical shells with complex boundary conditions. *Thin-Walled Structures*, Vol. 136, 2019, pp. 200–220.
- [28] Ghasemi, M. R., N. Shabakhty, and M. H. Enferadi. Vibration control of offshore jacket platforms through shape memory alloy pounding tuned mass damper (SMA-PTMD). *Ocean Engineering*, Vol. 191, 2019, id. 106348.
- [29] Konar, T. and A. D. Ghosh. Flow damping devices in tuned liquid damper for structural vibration control: a review. *Archives of Computational Methods in Engineering*, Vol. 28, 2021, pp. 2195–2207.
- [30] Zhang, Z., A. Staino, B. Basu, and S. R. K. Nielsen. Performance evaluation of full-scale tuned liquid dampers (TLDs) for vibration control of large wind turbines using real-time hybrid testing. *Engineering Structures*, Vol. 126, 2016, pp. 417–431.
- [31] Jahangiri, V. and C. Sun. Three-dimensional vibration control of offshore floating wind turbines using multiple tuned mass dampers. *Ocean Engineering*, Vol. 206, 2020, id. 107196.
- [32] Yang, J. and E. He. Coupled modeling and structural vibration control for floating offshore wind turbine. *Renewable Energy*, Vol. 157, 2020, pp. 678–694.
- [33] Yang, J., E. He, and Y. Hu. Dynamic modeling and vibration suppression for an offshore wind turbine with a tuned mass damper in floating platform. *Applied Ocean Research*, Vol. 83, 2019, pp. 21–29.

- [34] Hussan, M., M. S. Rahman, F. Sharmin, D. Kim, and J. Do. Multiple tuned mass damper for multi-mode vibration reduction of offshore wind turbine under seismic excitation. *Ocean Engineering*, Vol. 160, 2018, pp. 449–460.
- [35] Vandiver, J. K. and S. Mitome. Effect of liquid storage tanks on the dynamic response of offshore platforms. *Applied Ocean Research*, Vol. 1, No. 2, 1979, pp. 67–74.
- [36] Lee, H. H., S. H. Wong, and R. S. Lee. Response mitigation on the offshore floating platform system with tuned liquid column damper. *Ocean Engineering*, Vol. 33, No. 8, 2006, pp. 1118–1142.
- [37] Jin, Q., X. Li, N. Sun, J. Zhou, and J. Guan. Experimental and numerical study on tuned liquid dampers for controlling earthquake response of jacket offshore platform. *Marine Structures*, Vol. 20, No. 4, 2007, pp. 238–254.
- [38] Lotfollahi-Yaghin, M. A., H. Ahmadi, and H. Tafakhor. Seismic responses of an offshore jacket-type platform incorporated with tuned liquid dampers. *Advances in Structural Engineering*, Vol. 19, No. 2, 2016, pp. 227–238.
- [39] Yue, Q., L. Zhang, W. Zhang, and T. Kärnä. Mitigating iceinduced jacket platform vibrations utilizing a TMD system. *Cold Regions Science Technology*, Vol. 56, No. 2–3, 2009, pp. 84–89.
- [40] Taflanidis, A. A., D. C. Angelides, and J. T. Scruggs. Simulationbased robust design of mass dampers for response mitigation of tension leg platforms. *Engineering Structures*, Vol. 31, No. 4, 2009, pp. 847–857.
- [41] Chandrasekaran, S., D. Kumar, and R. Ramanathan. Dynamic response of tension leg platform with tuned mass dampers. *Journal of Naval Architecture Marine Engineering*, Vol. 10, No. 2, 2013, pp. 149–156.
- [42] Deng, W., J. Xu, X.-Z. Gao, and H. Zhao. An enhanced MSIQDE algorithm with novel multiple strategies for global optimization problems. *IEEE Transactions on Systems, Man, and Cybernetics: Systems*, Vol. 52, No. 3, 2022, pp. 1578–1587.
- [43] Deng, W., S. Shang, X. Cai, H. Zhao, Y. Song, and J. Xu. An improved differential evolution algorithm and its application in optimization problem. *Soft Computing*, Vol. 25, No. 7, 2021, pp. 5277–5298.
- [44] Deng, W., S. Shang, X. Cai, H. Zhao, Y. Zhou, H. Chen, et al. Quantum differential evolution with cooperative coevolution framework and hybrid mutation strategy for large scale optimization. *Knowledge-Based Systems*, Vol. 224, 2021, id. 107080.
- [45] Zhao, H., H. Liu, Y. Jin, X. Dang, and W. Deng. Feature extraction for data-driven remaining useful life prediction of rolling bearings. *IEEE Transactions on Instrumentation* and Measurement, Vol. 70, 2021, pp. 1–10.
- [46] Den Hartog, J. P. *Mechanical vibrations*, 4th edn. Dover, New York, 1985.