

Investigation of underwater shield tunnel excavation face stability in lower dense and upper loose strata

Fei Jia

Beijing University of Technology

Chuang Wang

Beijing University of Technology

Pengfei Li

lpf@bjut.edu.cn

Beijing University of Technology

Xiaopu Cui

Beijing University of Technology

Qing Xu

Beijing University of Technology

Zhaoguo Ge

China Railway Construction Corporation (China)

Research Article

Keywords: Lower dense and upper loose strata, Underwater shield tunnel, Stability of the excavation face, Various depths

Posted Date: February 9th, 2026

DOI: <https://doi.org/10.21203/rs.3.rs-8760248/v1>

License:  This work is licensed under a Creative Commons Attribution 4.0 International License.

[Read Full License](#)

Additional Declarations: No competing interests reported.

1 **Investigation of underwater shield tunnel excavation face stability in**
2 **lower dense and upper loose strata**

3 Fei Jia^{a, b}, Chuang Wang^a, Pengfei Li^{a, *}, Xiaopu Cui^a, Qing Xu^a, Zhaoguo Ge^c

4 ^a *Key Laboratory of Urban Security and Disaster Engineering, Ministry of Education, Beijing*
5 *University of Technology, Beijing 100124, China;*

6 ^b *China Railway No.3 Engineering Group No.4 Engineering Co., Ltd., Beijing 102300, China;*

7 ^c *China Railway 14th Corporation Mega Shield Construction Engineering Co. Ltd., Nanjing 211800,*
8 *China.*

9 *Corresponding author. E-mail address: lpf@bjut.edu.cn

10 **Abstract:** In order to study the stability of the excavation face in the lower dense and
11 upper loose, saturated sandy-pebble strata, physical model tests are conducted. The
12 study concentrated on researching the progressing failure laws of the shield tunnel
13 excavation face under various buried depths, and numerical simulations are employed
14 to confirm the test results. Meanwhile, the theory calculation model of excavation face
15 adapted to this stratum is put forward, and the theoretical formula of limited effective
16 support compressive stress is presented. The results indicated that, as the baffle moves,
17 the peak displacements of surface settlement successively occur in stages of no
18 settlement, slow settlement and rapid settlement. The decrease of buried depth will
19 increase the magnitude and range of surface settlement and will break the limiting state
20 of equilibrium of the strata faster. Simultaneously, the decrease of buried depth will
21 accelerate the seepage velocity of water in the strata without affecting the range of
22 seepage path of water. In addition, the decreased burial depth will increase unstable
23 range of the stratum. Under the equal burial depth, the unstable range of the lower dense
24 and upper loose is bigger than that of homogeneous strata. Finally, the limit effective
25 support compressive stress decreases with reduced burial depth.

26 **Keywords:** Lower dense and upper loose strata; Underwater shield tunnel; Stability of
27 the excavation face; Various depths

28 **1 Introduction**

29 When traversing rivers, lakes, and seas, the construction of underwater shield
30 tunnels offers distinct advantages over traditional bridge construction, including
31 minimal disruption to water traffic, resilience against adverse weather conditions, and
32 flexibility in terms of construction location. It is very important that the excavation face
33 is stable when building an underwater shield tunnel. This is because it affects how safe
34 the construction process is and how stable the tunnel will be in the long term (Zhang et
35 al. 2022a; Di et al. 2022).

36 Currently, the excavation stability of tunnels is typically studied using theory
37 analysis, numerical simulation, and model tests. Theoretical analysis methods can be
38 applied to various geological conditions and clarify the instability mechanisms of
39 excavation faces. The two main theoretical analysis methods are the limit equilibrium
40 method (Ding et al. 2022; Wang et al. 2023a; Li et al. 2023; Lei et al. 2024) and the
41 limit analysis method (Yang and Zhong 2019; Yi et al. 2019; Antão et al. 2021; Cheng
42 et al. 2023a; Kong et al. 2024; Yang et al. 2024). The limit equilibrium method is based
43 on the assumption that the excavation face of a tunnel is in a critical state, and proposes
44 a potential failure mechanism. For example, Han et al. (2021) proposed a stability
45 model of excavation face which is suitable for crossing the fault fracture zone of high
46 hydraulic pressure, which is composed of a trapezoid and a prism. Liu et al. (2019)
47 proposed an excavation face failure model consisting of rotational and gravitational
48 damage zones for sand strata. The limit analysis method, based on plastic theory, solves
49 for the limit support force of the excavation face by applying the upper-bound theorem
50 (Ding et al. 2019; Zhang et al. 2019; Cui et al. 2025a) and lower-bound theorem
51 (Habumuremyi and Xiang 2023). Meanwhile, the limit analysis method is a more
52 accurate way of describing how the excavation face fails when there is seepage (Li et
53 al. 2021; Hou and Yang 2022).

54 Numerical simulation method exhibits strong adaptability in addressing complex
55 geological conditions and multi-field coupling issues. It is based on the finite element
56 method (Alagha and Chapman 2019; Ma et al. 2022b; Ge et al. 2024; Chen et al. 2024),
57 finite difference method (Ye et al. 2022; Cheng et al. 2023b; Cui et al. 2024) and
58 discrete element method (Wang et al. 2022; Fu et al. 2022) to simulate and analyze the
59 excavation face of shield tunnel in two-dimensional or three-dimensional. Among them,
60 the finite element method can be coupled with the physical field such as seepage field,

61 which is suitable for the analysis of the stability of the excavation face in saturated
62 strata (Lu et al. 2017; Wang et al. 2019). The discrete element method can deal with the
63 motion process of discrete particles well, and is suitable for simulating local failure and
64 collapse in the process of excavation face instability. For sand-gravel inclined strata, Tu
65 et al. (2024) investigated the effect of the inclined angle of the strata on the limit support
66 force of the excavation face. Wang et al. (2024) obtained the law that with the increase
67 of cutterhead opening rate and rotating speed, the local failure area in cobble-rich soil
68 gradually increases.

69 The model test method can visually show the progressive instability process of
70 strata, which is convenient for observing the failure mechanism of the excavation face.
71 Gravity model test (Hu et al. 2021; Di et al. 2024) and centrifugal model test (Wong et
72 al. 2012; Yin et al. 2021) are commonly used in physical model test. Due to the low
73 cost of gravity model tests and ease of repetition, scholars have done plenty of studies
74 about the stability of excavation faces for sand strata (Lü et al. 2018; Zhao et al. 2024)
75 and clay strata (Ma et al. 2022a; Jia et al. 2023). The centrifugal model test's stress field
76 aligns with standard practice, offering a more authentic reflection of strata failure
77 processes. Through a series of centrifugal model tests, Chen et al. (2018) obtained the
78 impact of different water pressure on the limit support force of excavation face in sand
79 strata. Weng et al. (2020) obtained the progressive failure mechanism of excavation
80 face under different longitudinal slope angles for clay strata. Cui et al. (2025b) studied
81 the failure mechanism of excavation surfaces in inclined water-rich strata with different
82 inclination angles. Cui et al. (2025c) also investigated the failure mechanism of
83 excavation surfaces in water-rich, silty clay overlying sandy cobble strata under
84 differing seepage conditions.

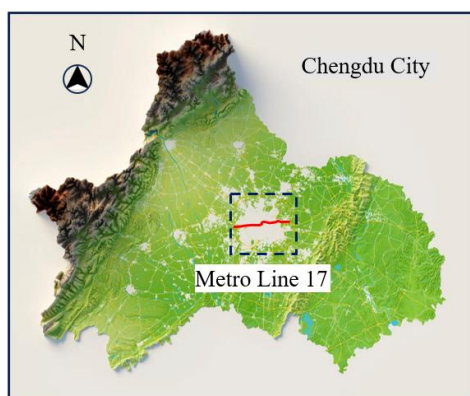
85 Sandy pebble strata is widely distributed in Beijing, Chengdu and other cities in
86 China. The sandy pebble strata are characterized by uneven particle size, large porosity
87 and good water permeability. Due to the strong dispersibility of sandy pebble strata, it
88 is significantly different from the engineering properties of sand strata and clay strata
89 (Wang et al. 2023b). If the shield tunnel is constructed in saturated sandy pebble strata,
90 phenomena such as leakage of water and ground collapse are likely to occur. Due to the
91 strata deposition, the actual sandy pebble strata are usually loose in the upper part and
92 dense in the lower part, but the current researches only focus on the homogeneous sandy
93 pebble strata (Lin et al. 2021; Di et al. 2023). Meanwhile, the burial depth will have a

94 important effect on the failure mechanism for excavation face (Zhang et al. 2022b; Liu
95 et al. 2024).

96 This study focuses on a section of Chengdu Metro Line 17 as the engineering
97 background, utilizing model tests to investigate the lower dense and upper loose
98 saturated sandy pebble strata. Numerical simulations are developed to compare and
99 verify the results of model tests. By combining model tests and numerical simulations,
100 this research aims to explore the progressive failure laws of shield tunnel excavation
101 face with active instability for various buried depths. Meanwhile, a theoretical
102 calculation model suitable for this formation is proposed, and the analytical formula of
103 the limit effective support pressure on excavation face under the seepage condition is
104 derived. This is of great significance to ensure the construction safety of similar projects.

105 **2 Project Background**

106 The dual-track tunnel of Chengdu Metro Line 17 Jiujiang North station to Baifo
107 Bridge station passes under the Jiang 'an River, and the metro tunnel is constructed by
108 shield method. The tunnel is 7.5 meters wide, and the distance from the top of the tunnel
109 to the bottom of the river is about 15 meters. The strata through which the tunnel passes
110 are mainly slightly, medium and dense sandy pebble strata. The tunnel is primarily
111 driven at the junction of the medium-dense and dense sandy pebble strata. The left line
112 tunnel is selected, and the geographical location of the shield section and stratigraphic
113 profile are shown in Fig. 1, and Table 1 shows the physical and mechanical parameters
114 of the stratum.



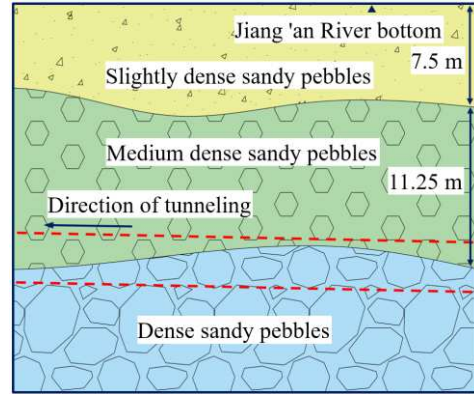
(a) Metro line 17



(b) Jiujiang North station-Baifo Bridge station



(c) Geographic location of the Jiang'an River



(d) Stratigraphic profile

Fig. 1. Geographical location of the shield section and stratigraphic profile.

115

Table 1. Physical and mechanical parameters of the strata.

Classification of strata	Saturated unit weight γ (kg/m ³)	Internal friction angle φ (°)	Young's modulus E (MPa)	Poisson's ratio μ	Relative compactness D_r
Slightly dense sandy pebble	1900	38	18	0.27	0.33
Medium dense sandy pebble	2100	42	38	0.24	0.57
Dense sandy pebble	2300	45	50	0.22	0.78

116

3 Test design

117

3.1 Test device and scheme

118

The stability of the excavation face is studied using an indoor model test device (Mi and Xiang 2020), as illustrated in Fig. 2. The model box side wall is made of a transparent acrylic plate, and a semi-cylindrical shield tunnel with an inner diameter of 30 cm has been set up on it. The excavation face control system is composed of a fixed plastic plate with holes and a movable baffle, and the plastic plate with holes is used to simulate the cutterhead during shield excavation. The baffle is made of wire mesh and sponge. This allows water to pass through while preventing soil from doing so. The water is returned to the strata surface by a water pump through the baffle, so that the water level is maintained at 1200 mm during the entire test. The plate is connected with a runner through a bearing. Rotating the runner moves the baffle backward, resulting in insufficient support force and active instability of the excavation face. In order to study the influence of buried depth on the stability of excavation face, three conditions of buried depth $H/D = 2, 1.5$ and 1 are used for test, where H is the thickness of soil cover

130

131 and D is the diameter of tunnel. Under the three burial depth conditions, the distance of
 132 water level above the surface is defined as H_w . The thickness of slightly dense sandy
 133 pebble, medium dense sandy pebble and dense sandy pebble are defined as H_1 , H_2 and
 134 H_3 , respectively. Among them, the thickness ratio between the slightly dense sandy
 135 pebble and the medium dense sandy pebble is 1:1.5, and the thickness of various strata
 136 is shown in Table 2.

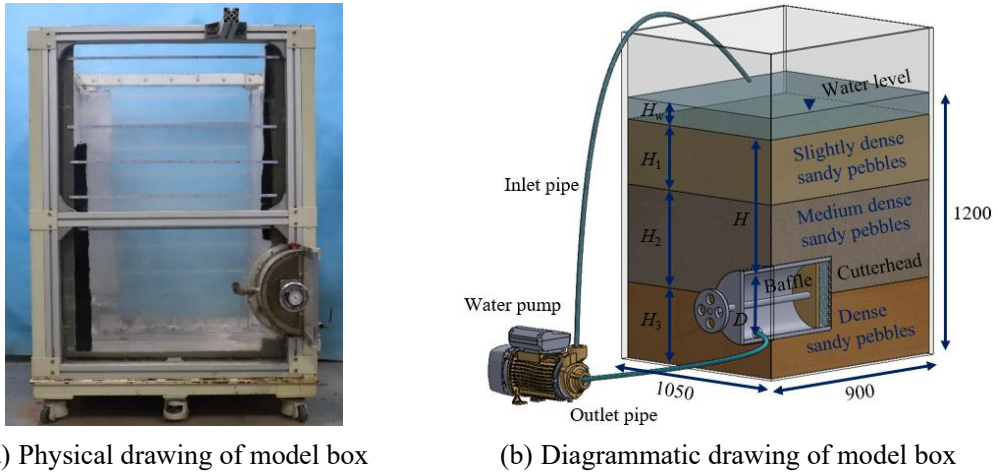


Fig. 2. The tunnel excavation stability indoor model test device. Unit: mm

Table 2. The thickness of each stratum for various burial depths. Unit: mm

Test condition	H_w	H_1	H_2	H_3
$H/D = 2$	100	300	450	350
$H/D = 1.5$	250	240	360	350
$H/D = 1$	400	180	270	350

3.2 Test materials and procedures

139 In the model tests, the soil is graded soil and prepared according to the law of
 140 similarity (Li et al. 2025). The internal friction angles for the three soils are obtained
 141 from straight shear tests. The relative compactness D_r of slightly dense sandy pebble,
 142 medium dense sandy pebble and dense sandy pebble are 0.35, 0.55 and 0.75,
 143 respectively.

144 The test process is shown in Fig. 3, and the specific test steps are as follows:

145 (1) Clean the model box. Apply vaseline to the side walls of the model box to
 146 reduce the friction between the soil particles and the side walls.

147 (2) Carry out soil filling and leveling. According to the D_r of the three strata, the
 148 filling quality of each is calculated. During the filling process, the earth pressure boxes
 149 and osmometers are buried in the designed position, and the strata is saturated with
 150 water. When the soil is filled to a height of 350 mm, lay a strip of colored sand. And

151 starting from 500 mm, every 100 mm lay a strip of colored sand. Colored sand is used
 152 to observe the displacement in the strata during the test. When the height of the strata
 153 reaches the predetermined position, the surface is leveled.

154 (3) Connect the data acquisition device. The surface displacement meters are set
 155 up on the surface, and the static strain collector and osmotic collector are connected.
 156 The static strain collector obtains the surface settlement data and earth pressure data,
 157 and the osmometer collector obtains the water pressure data.

158 (4) Conduct the tests. Turn the runner counterclockwise to move the baffle
 159 backward at the speed of about 1 mm/s. DIC instrument is used to monitor strain and
 160 displacement of the strata throughout the test. The test is finished when the baffle has
 161 moved 10 cm.

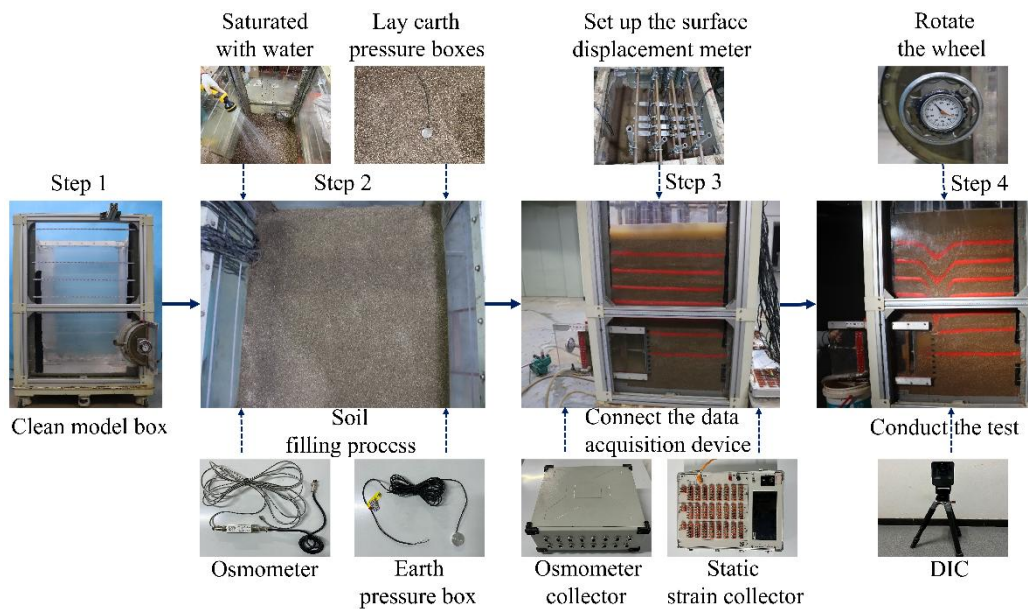


Fig. 3. Test process.

162 **3.3 Monitoring point arrangement**

163 As shown in Fig. 4, 16 surface displacement monitoring points have been arranged
 164 on the strata surface to monitor changes in surface settlement.

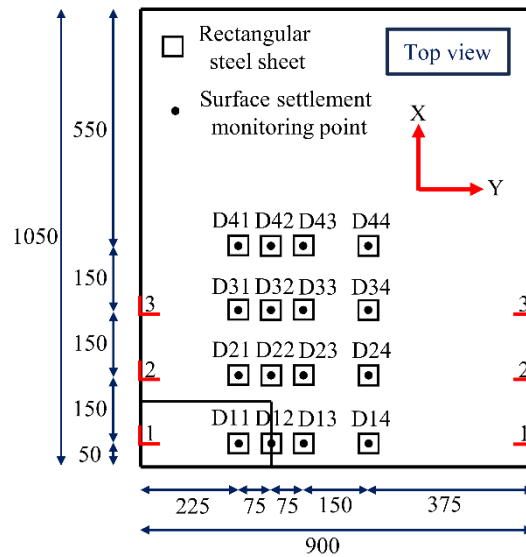


Fig. 4. Distribution of surface settlement monitoring points. Unit: mm

165 When $H/D = 2$ and $H/D = 1.5$, the arrangement of vertical soil pressure boxes is
 166 shown in Fig. 5, with a total of 23 earth pressure boxes. When $H/D = 1$, the vertical
 167 earth pressure boxes in the strata are arranged as shown in Fig. 6. There are 16 earth
 168 pressure boxes in total, which are used to monitor the change law of earth pressure in
 169 the strata.

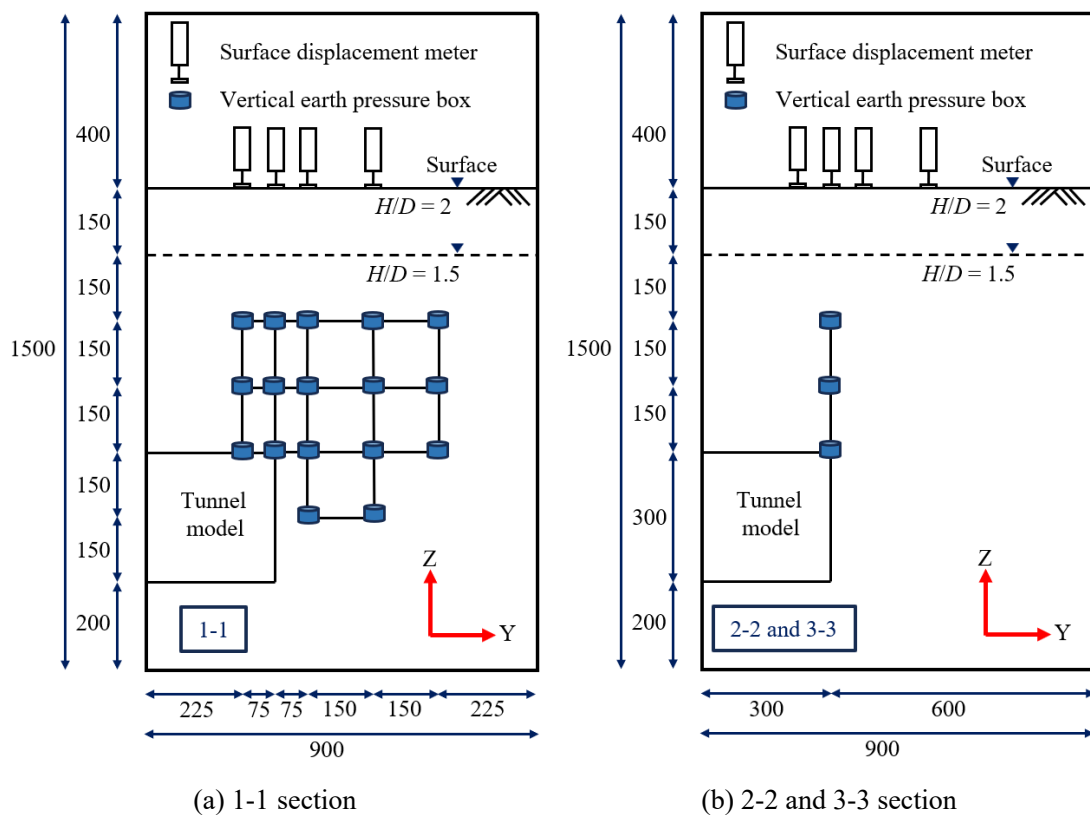


Fig. 5. Distribution of earth pressure boxes in the strata for $H/D = 2$ and $H/D = 1.5$. Unit: mm

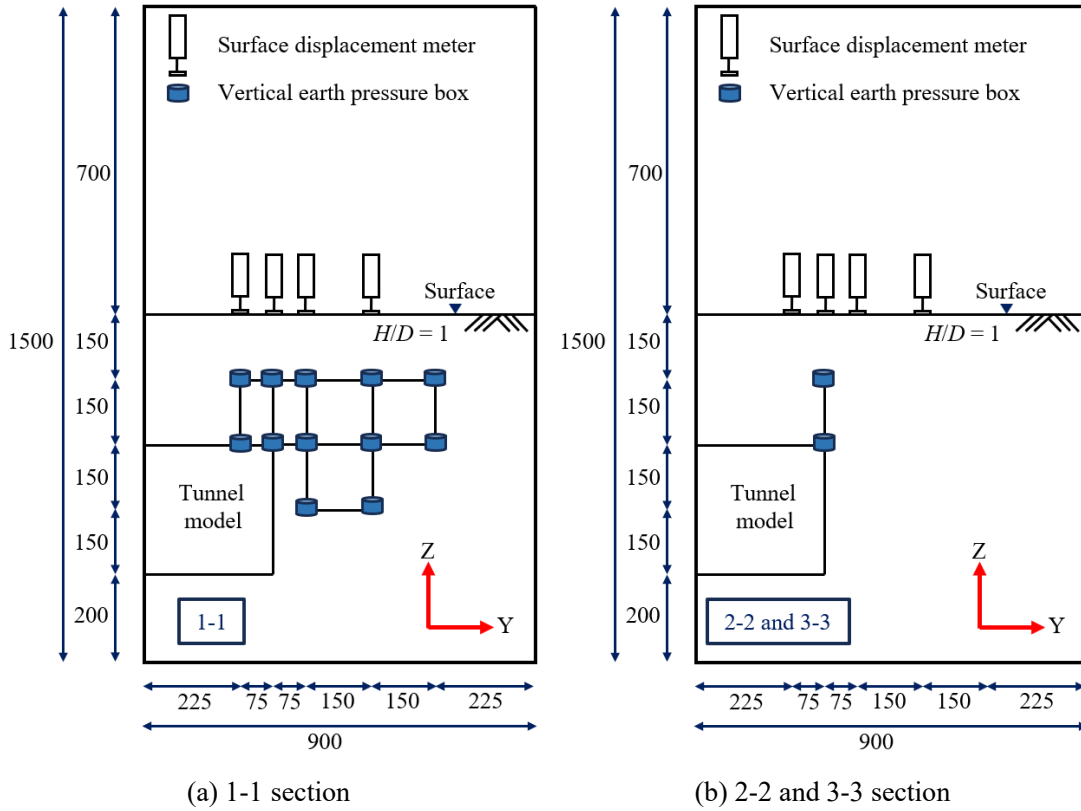


Fig. 6. Distribution of earth pressure boxes in the strata for $H/D = 1$. Unit: mm

170 6 earth pressure boxes and 4 osmometers are dispersed on the cutterhead, while 5
 171 osmometers are dispersed on the side wall of the model box in front of the excavation
 172 face. The arrangement of earth pressure boxes and osmometers are shown in Fig. 7.

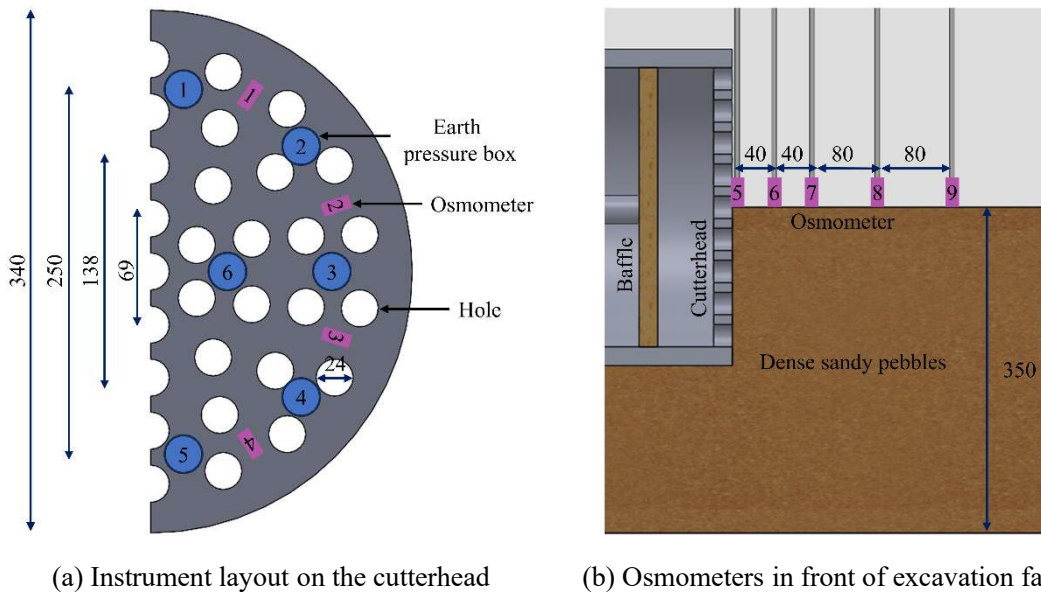


Fig. 7. The arrangement of earth pressure boxes and osmometers. Unit: mm

173 3.4 Numerical model establishment

174 Table 2 also shows the thickness of the three strata under various burial depths, as
 175 established using ABAQUS software. The soil permeability coefficient $k = 2 \times 10^{-5}$ m/s,

176 which is obtained from the constant head permeability test, is used in the numerical
177 simulations.

178 The steps of numerical simulation are as follows:

179 (1) A numerical model corresponding to the model test dimensions was established
180 based on the corresponding burial depth, as shown in Fig. 8. The tunnel is partially
181 empty and the lining unit supports it. The material's properties are essentially consistent
182 with those of the soil in the model tests. After setting the corresponding boundary
183 conditions, the geo-stress balance is carried out.

184 (2) The excavation face moves backwards at a rate of 0.002 mm each time and
185 fluid-structure coupling calculations are performed.

186 (3) For each 1 mm movement, the excavation face's restriction condition is
187 converted to a normal fixed restriction, and the fluid-structure coupling computation is
188 then repeated until the equilibrium state is reached. The numerical simulation is
189 finished when the movement distance reaches 10 cm.

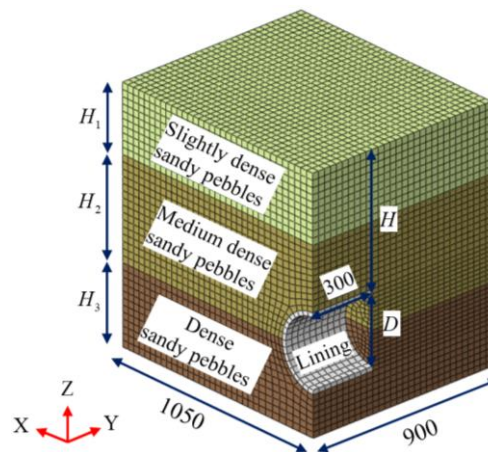


Fig. 8. Numerical model. Unit: mm

190 4 Test results analysis

191 4.1 Surface settlement analysis and soil arch development

192 The change process of the soil displacement increment field at various burial
193 depths is acquired by the analysis of the DIC instrument, as illustrated in Figs. 9–11.
194 Points A, B, and C, respectively, are the places where the highest displacement of
195 ground settlement occurs under three distinct burial depth environments.

196 There are three stages to the peak displacement change process, regardless of
197 whether they are model tests or numerical simulations. Figs. 12–14 display the peak
198 displacement change law with L . Under different burial depths, the corresponding

199 ranges of L in the three stages are shown in Table 3.

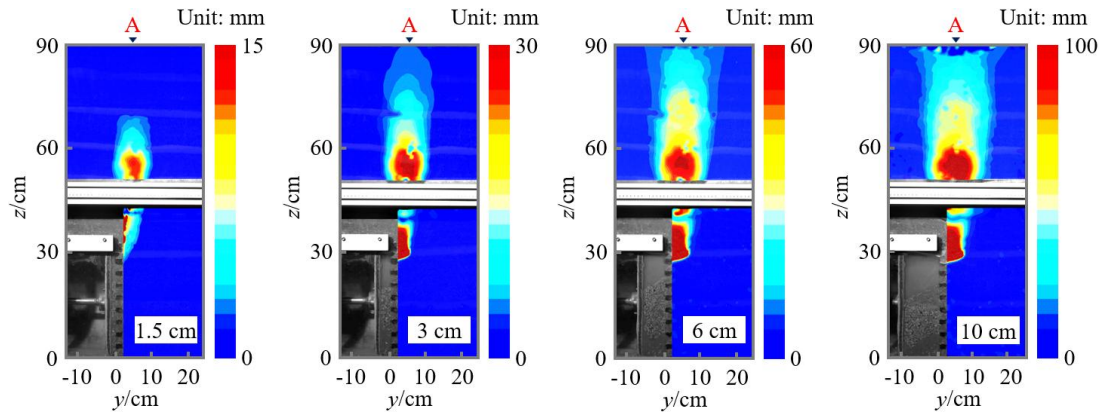


Fig. 9. The change law of displacement increment field with L for $H/D = 2$.

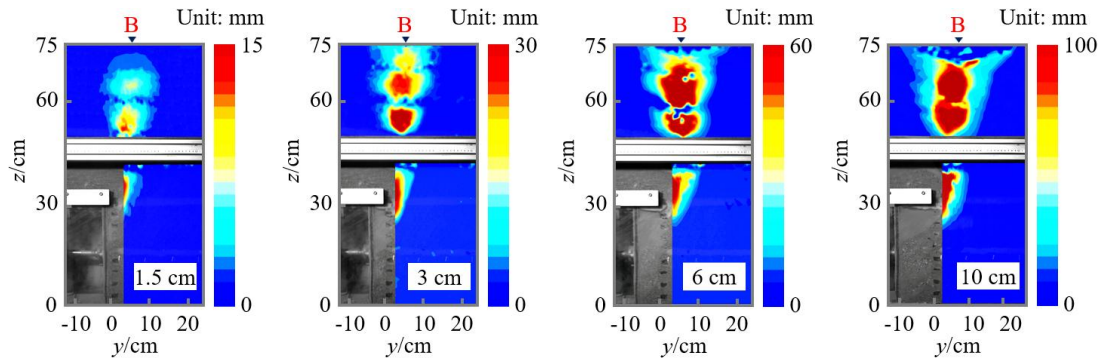


Fig. 10. The change law of displacement increment field with L for $H/D = 1.5$.

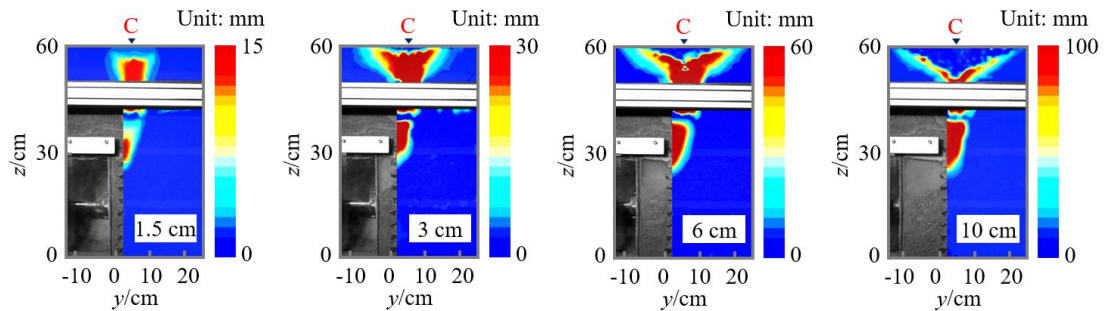


Fig. 11. The change law of displacement increment field with L for $H/D = 1$.

200

Table 3. The range of L in each stage for various burial depths.

Test condition		L (cm)		
		First phase	Second phase	Third phase
Model test	$H/D = 2$	0-2	2-3.5	3.5-10
	$H/D = 1.5$	0-1.6	1.6-2.5	2.5-10
	$H/D = 1$	0-1.3	1.3-1.9	1.9-10
Numerical simulation	$H/D = 2$	0-2.2	2.2-4	4-10
	$H/D = 1.5$	0-2	2-3.1	3.1-10
	$H/D = 1$	0-1.5	1.5-2.4	2.4-10

201

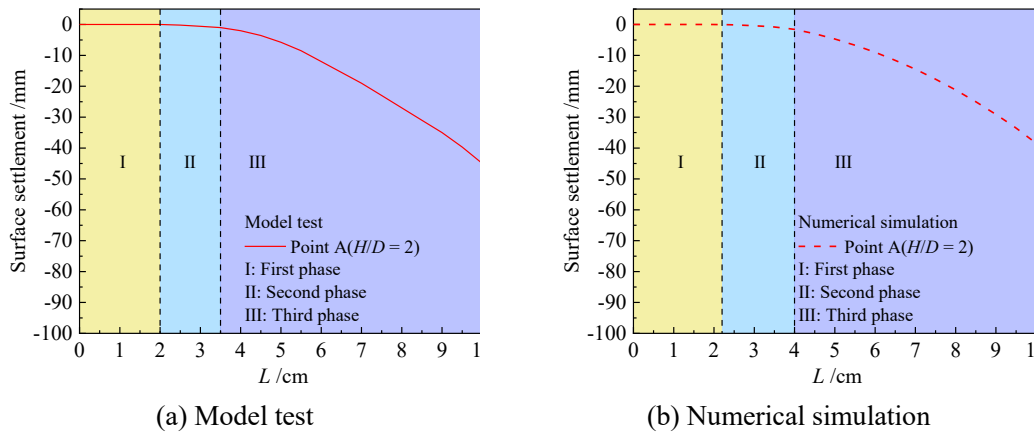


Fig. 12. The change law of peak displacement of surface settlement with L for $H/D = 2$.

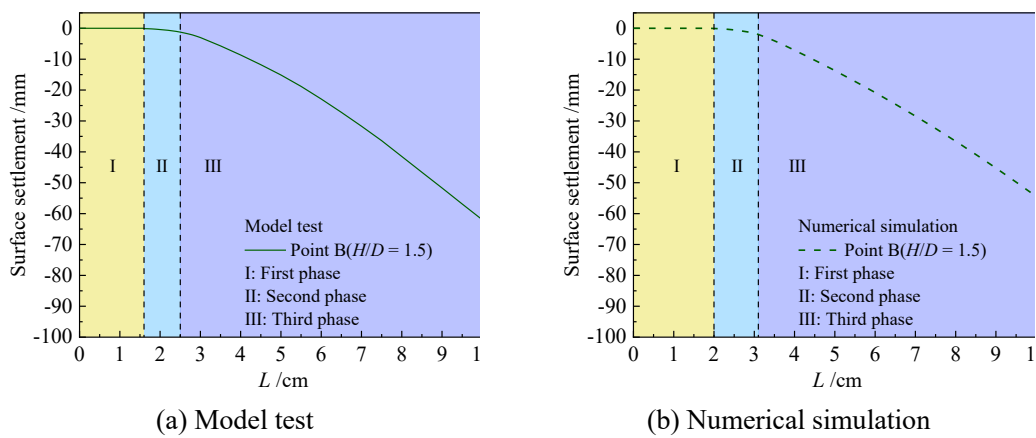


Fig. 13. The change law of peak displacement of surface settlement with L for $H/D = 1.5$.

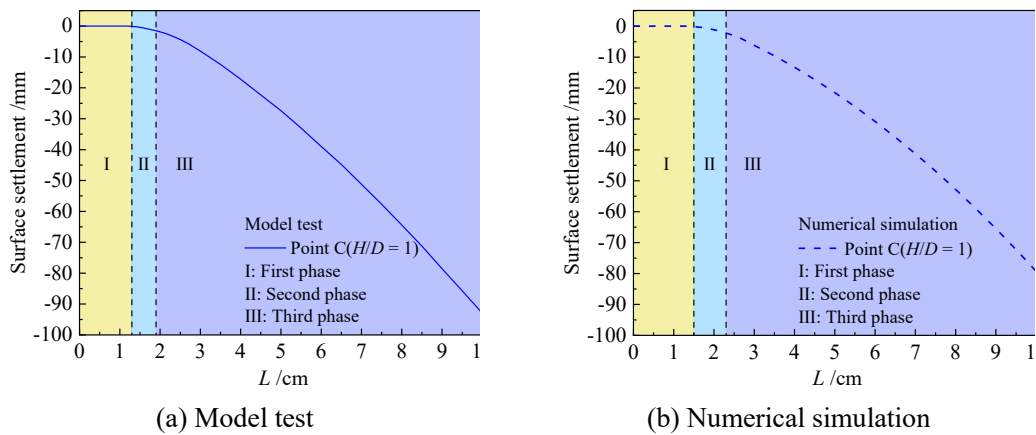


Fig. 14. The change law of peak displacement of surface settlement with L for $H/D = 1$.

202 (1) No settlement stage. The soil ahead of the excavation face experiences active
 203 instability as a result of the increase in L . Meanwhile, the soil arch effect begins to form
 204 and gradually develop in the strata. However, the soil arch has not yet developed to the
 205 surface, so the surface has not settled at this stage.

206 (2) Slow settlement stage. As L continues to increase, the soil arch effect develops
 207 to the surface. However, at this stage, the instability range of the stratum is mainly

208 increased, so slow settlement occurs at the surface.

209 (3) Rapid settlement stage. As the soil arch effect gradually fades, the strata
210 become generally unstable, and settlement spreads quickly.

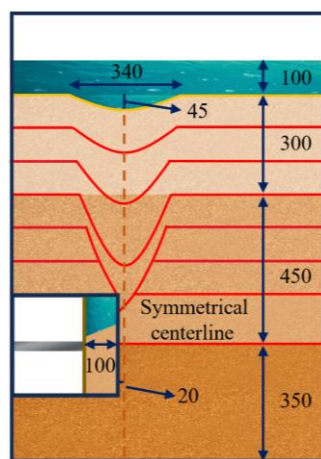
211 Meanwhile, with the decrease of burial depth, the peak displacement increases
212 gradually under the same L . In addition, under the same conditions, the settlement
213 values of numerical simulations are smaller than that of model tests. This is because the
214 soil material in numerical simulations is based on the assumption of continuous media,
215 while the soil material in model tests is relatively discrete and has discontinuity,
216 resulting in large surface settlement obtained in model tests.

217 4.2 Three-dimensional surface settlement analysis

218 Figs. 15–17 show the deformation results of the strata under different burial depths
219 when $L = 10$ cm. Under different burial depth conditions, three-dimensional surface
220 settlement is shown in Fig. 18.



(a) Physical drawing

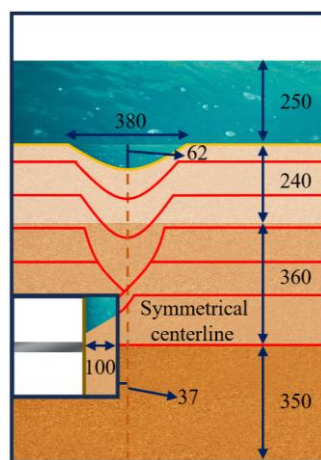


(b) Diagrammatic drawing

Fig. 15. The deformation result of the strata for $H/D = 2$. Unit: mm



(a) Physical drawing



(b) Diagrammatic drawing

Fig. 16. The deformation result of the strata for $H/D = 1.5$. Unit: mm

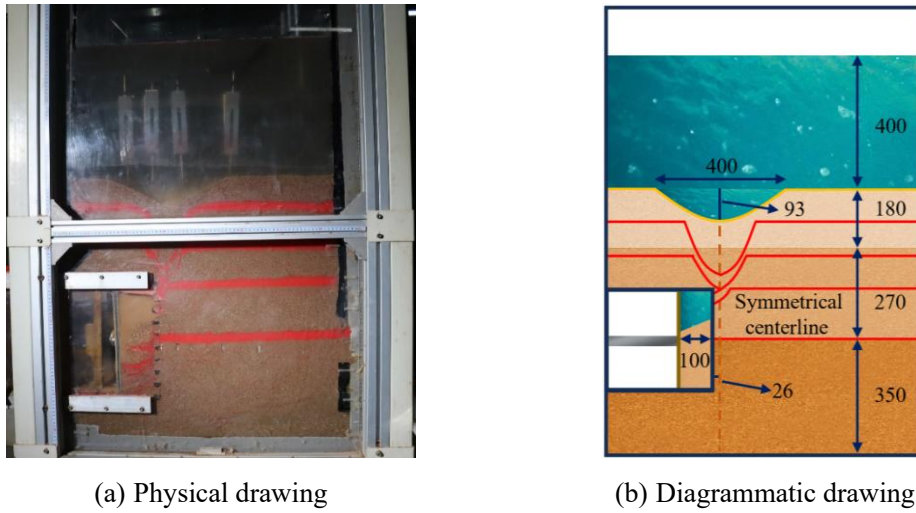


Fig. 17. The deformation result of the strata for $H/D = 1$. Unit: mm

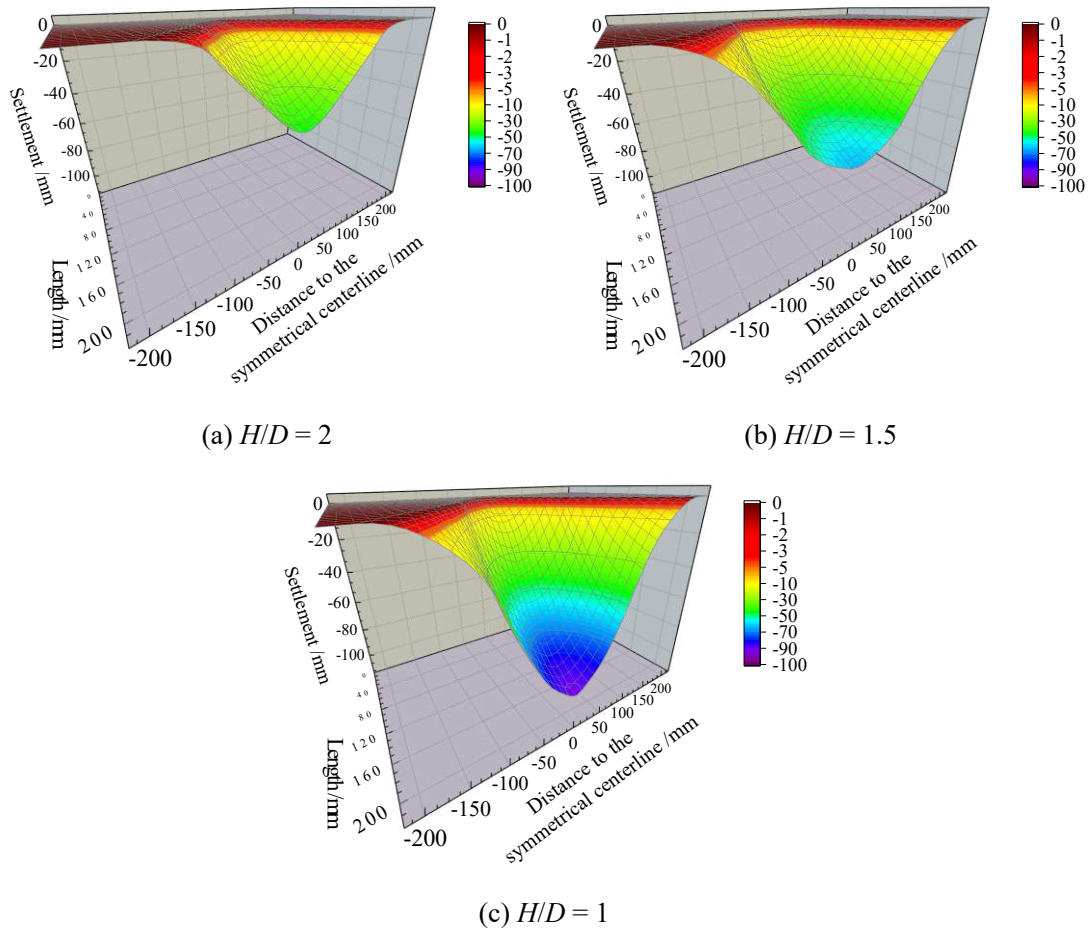


Fig. 18. Three-dimensional surface settlement for various burial depths.

221 When $L = 10$ cm, the surface creates a semi-funnel-shaped settlement area. The
 222 settlement funnel's symmetrical centerlines are situated ahead of the digging face, and
 223 it is 20 mm, 37 mm, and 26 mm away from the digging face at various buried depths.
 224 The diameter of the settlement funnel progressively increases to 34 cm ($1.13D$), 38 cm

225 (1.27D), and 40 cm (1.33D) as the buried depth decreases. The maximum settlement
 226 values are also gradually increasing, with values of 45 mm, 62 mm and 93 mm,
 227 respectively.

228 4.3 Seepage field analysis

229 Figs. 19–21 illustrate the changing rule of pressure in water with L at various burial
 230 depth settings. It is evident that each osmometer's water pressure exhibits a propensity
 231 to rise and then stabilize as L increases. In addition, the increase of water pressure of
 232 osmometer 9 furthest away from the excavation surface is relatively small. This shows
 233 that the seepage path range of water is basically same under different burial depths.
 234 Osmometers on the cutterhead and osmometers 5, 6, and 7 close to the excavation face
 235 show an increase in water pressure as the burial depth decreases. This shows that the
 236 decrease of the burial depth will increase the water seepage velocity.

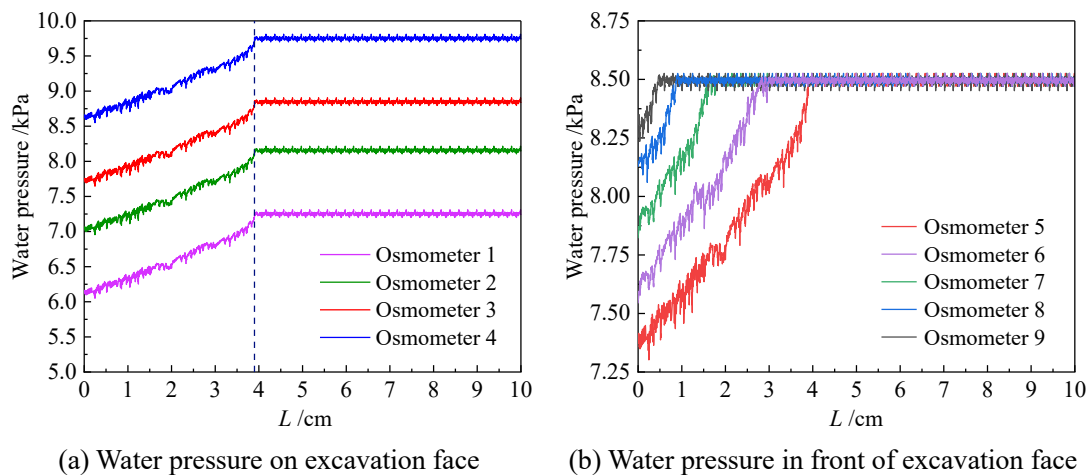


Fig. 19. The change law of water pressure with L for $H/D = 2$.

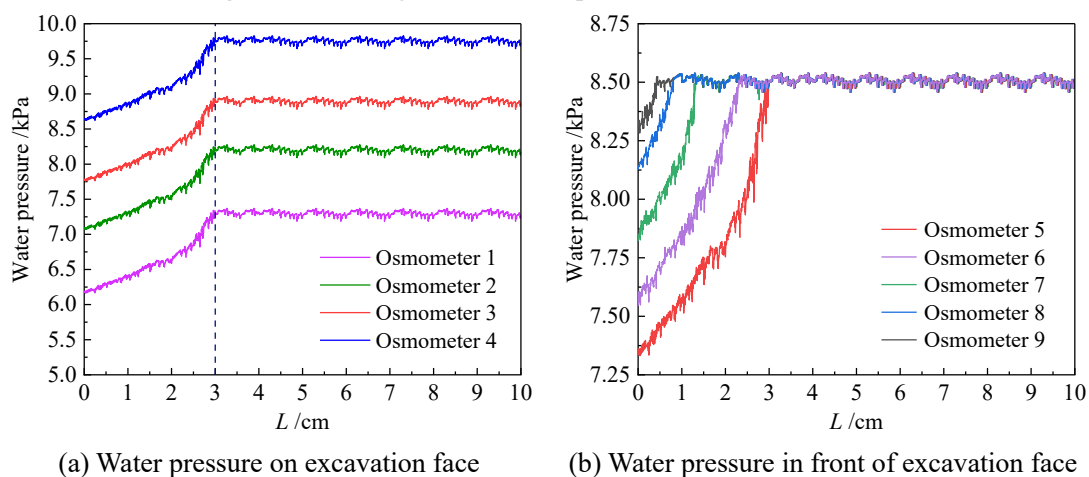
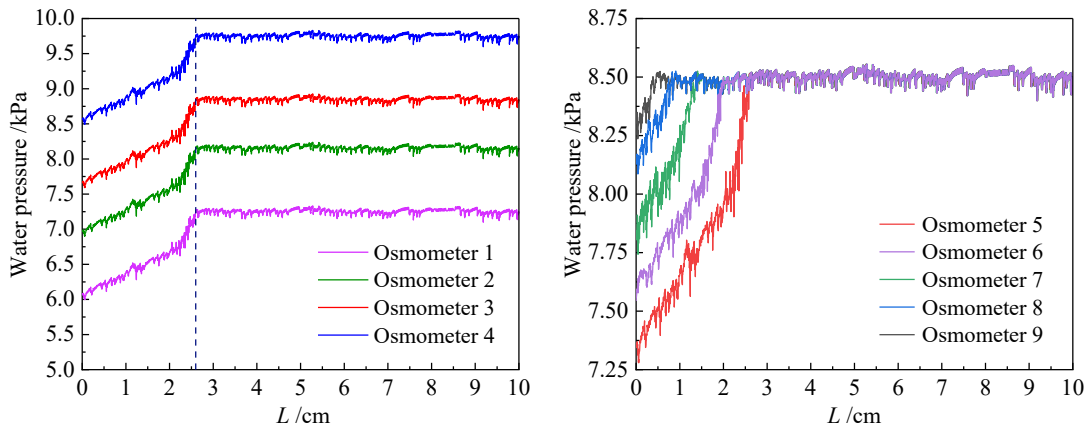


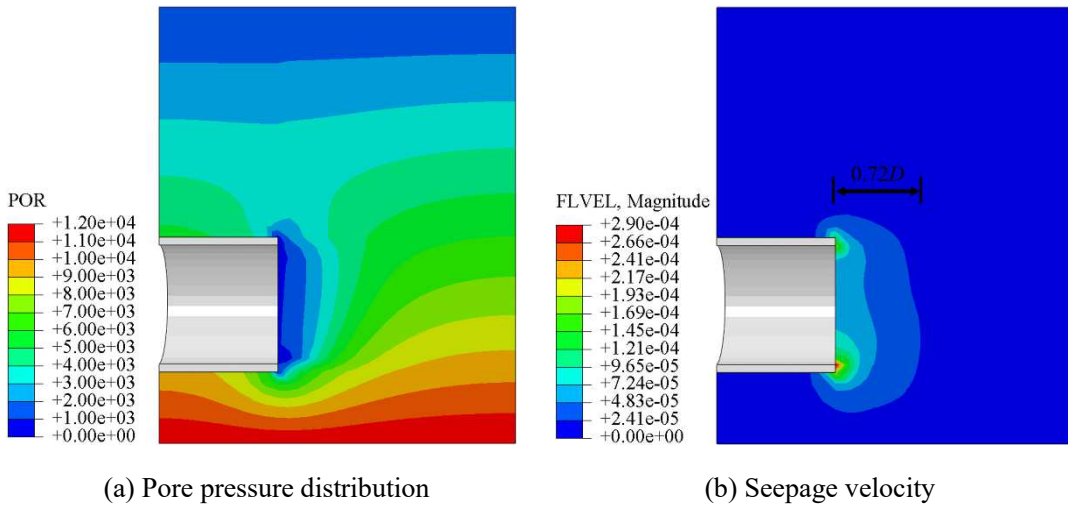
Fig. 20. The change law of water pressure with L for $H/D = 1.5$.



(a) Water pressure on excavation face (b) Water pressure in front of excavation face

Fig. 21. The change law of water pressure with L for $H/D = 1$.

237 In order to verify the above conclusions, the numerical simulation method is used
 238 for further analysis. The pore pressure distribution and seepage velocity of strata under
 239 different burial depths are shown in Figs. 22–24. While the far boundary continues to
 240 maintain hydrostatic pressure, ground water flows in the direction of the excavated area.
 241 Under different burial depth conditions, the scope of water seepage pathways is about
 242 $0\text{-}0.72D$, and this shows that the decrease of burial depth has essentially no effect on
 243 the seepage path range of water.



(a) Pore pressure distribution (b) Seepage velocity

Fig. 22. The pore pressure distribution and seepage velocity of strata for $H/D = 2$.

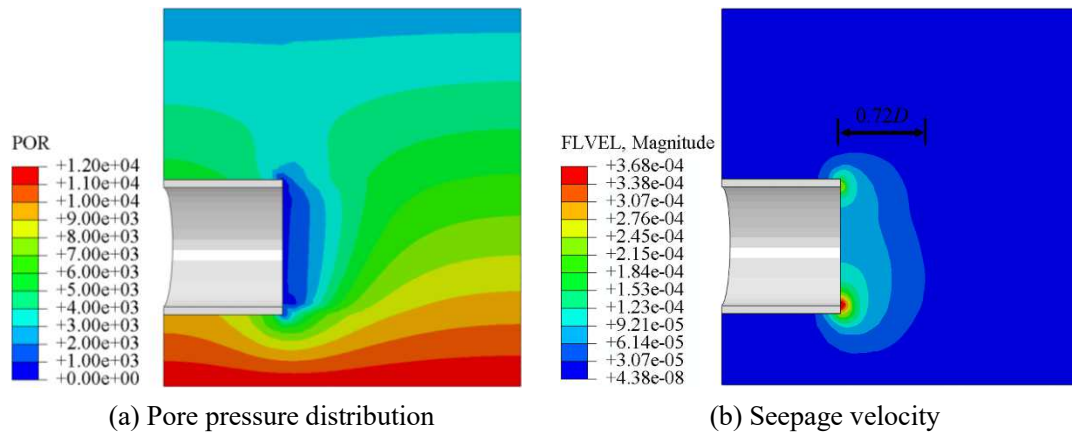


Fig. 23. The pore pressure distribution and seepage velocity of strata for $H/D = 1.5$.

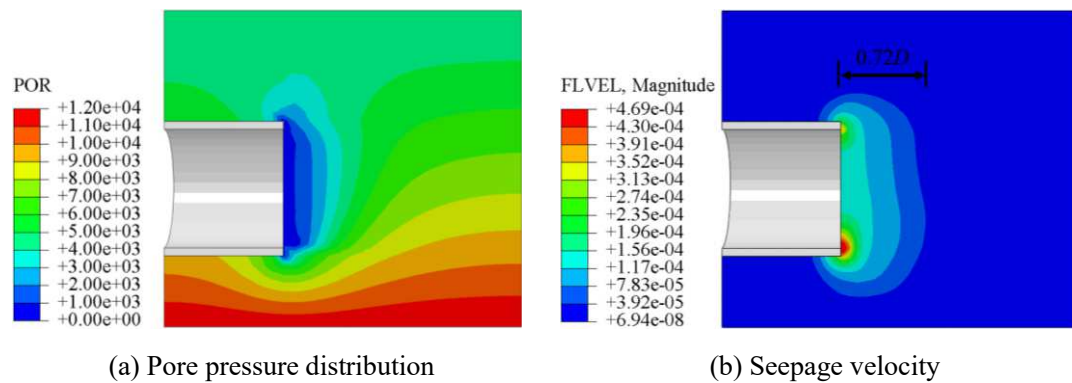


Fig. 24. The pore pressure distribution and seepage velocity of strata for $H/D = 1$.

244 Fig. 25 displays the changing law of seepage velocity on the excavated face along
 245 the diameter direction. Under different burial depths, the seepage velocity shows a
 246 tendency to decrease and then increase along the diameter of the excavated face. With
 247 z between 0 and 10 cm (0 and $D/3$), the seepage velocity progressively drops. With z
 248 between 10 and 30 cm ($D/3$ - D), the seepage velocity progressively rises. At the base of
 249 the excavated face, the seepage velocity is at its highest. This is because water flows
 250 from the area of high water pressure to the area of low water pressure, and the water
 251 pressure difference at the bottom of the excavation face is the largest, and the seepage
 252 velocity is the largest. And at the same z , the seepage velocity increases gradually with
 253 the decrease of burial depth. When the buried depth $H/D = 2, 1.5$ and 1 , the maximum
 254 seepage velocity is 2.90×10^{-4} m/s, 3.68×10^{-4} m/s and 4.69×10^{-4} m/s, respectively. This
 255 is because as buried depth increases, earth obstruction to water flow increases, slowing
 256 down the water's seepage velocity. The conclusion drawn from the model tests is in line
 257 with this.

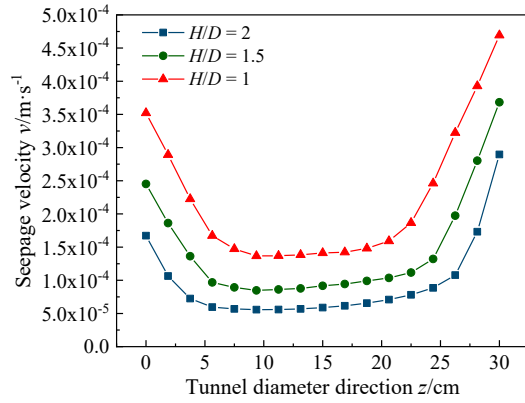


Fig. 25. The Seepage velocity of excavation face for various burial depths.

258 **4.4 Limit equilibrium state analysis of strata**

259 Fig. 26 illustrates the changing rule of soil pressure on the cutterhead with L at
 260 various buried depths.

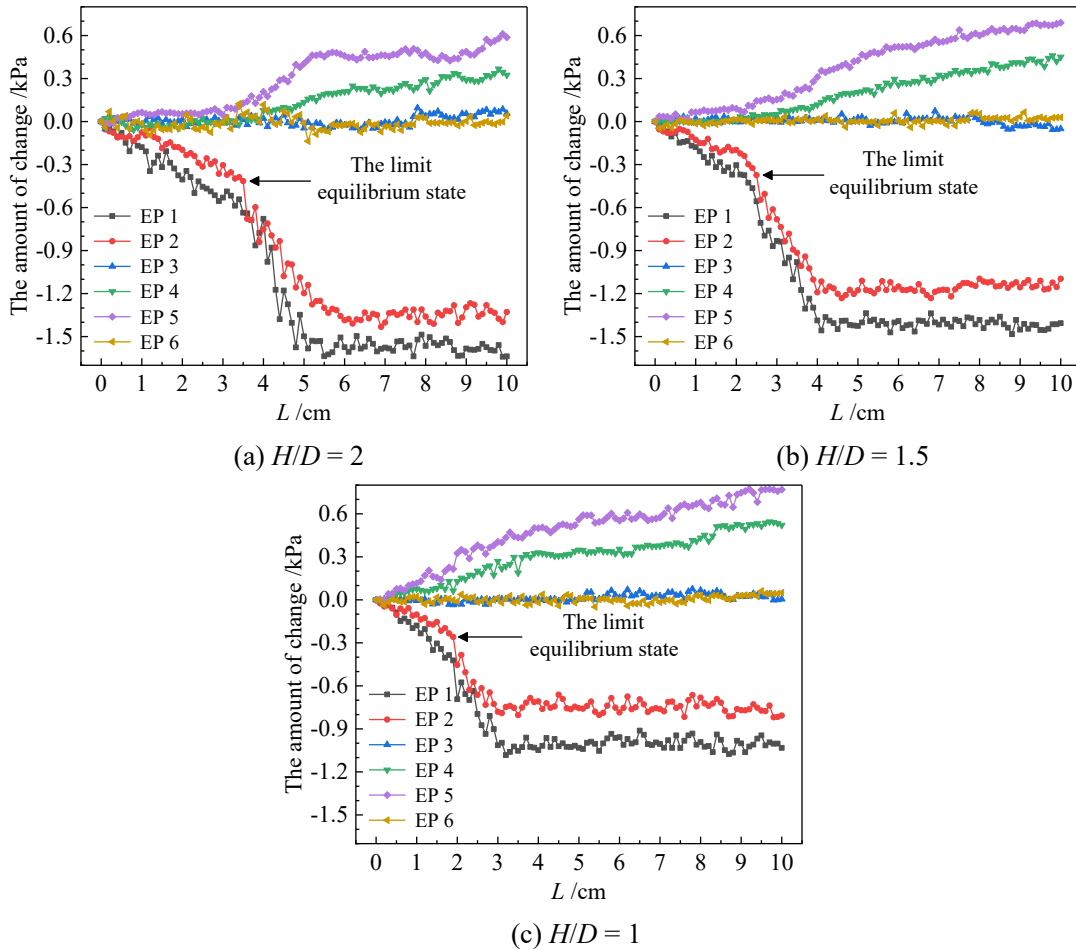


Fig. 26. The change law of earth pressure on cutterhead with L for various burial depths.

261 Under various buried depth circumstances, the values of EP 3 and EP 6 fixed at
 262 the center of the excavated face are essentially steady. The soil particles in the stratum
 263 enter the chamber through the opening hole in the upper portion of the cutterhead as

264 the baffle slides backwards during the whole test. Therefore, the instability of dense
265 sandy pebble stratum has not been occurred. In Figs. 15–17, the colored sand at 350
266 mm always maintains a straight line, which can also verify this conclusion.

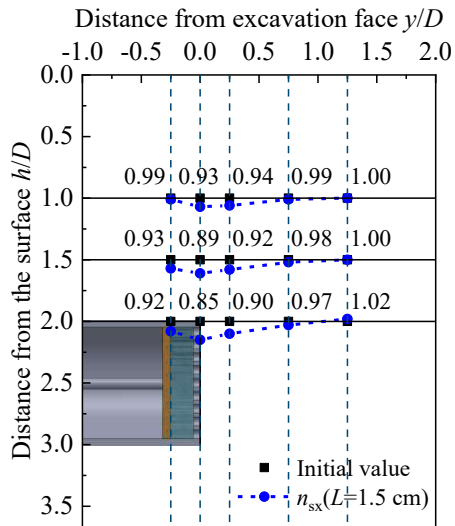
267 In the lower portion of the excavation face, the values of EP 4 and EP 5 increase
268 as L increases. Due to the increasing of soil particles entering the chamber, the
269 horizontal extrusion pressure acting on the lower part of cutterhead increases. When L
270 = 10 cm, with the decrease of buried depth, the increase amounts of EP 5 is 0.59 kPa,
271 0.69 kPa and 0.77 kPa, respectively. This suggests that the collapsed area over the
272 excavation face will expand as the buried depth decreases and the chamber's soil intake
273 increases.

274 The values of EP 4 and EP 5 fixed in the upper part of the excavation face shows
275 a trend of slow decline at first, then rapid decline and finally stability. The soil primarily
276 enters the soil bin through the opening hole in the top portion of the cutter head due to
277 the baffle's movement, which causes the values of EP 1 and EP 2 to gradually decrease.
278 The limit equilibrium state of the strata will be broken and there will be general
279 instability as L increases steadily. A small disturbance will cause a large amount of soils
280 to collapse, resulting in a rapid decrease in earth pressure. The comparable L values in
281 the limit state of equilibrium are 3.5 cm, 2.5 cm, and 1.9 cm, respectively, for $H/D = 2$,
282 1.5, and 1. This suggests that lowering the burial depth will cause the strata's limit
283 equilibrium condition to be broken more quickly, causing the strata to become unstable
284 overall sooner rather than later.

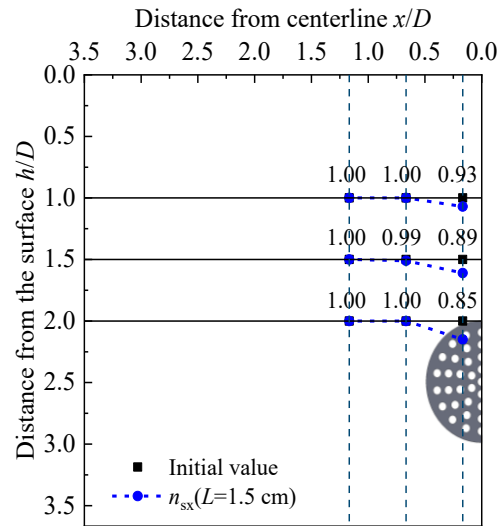
4.5 Instability pattern analysis of strata

285 Under the geological conditions where strata are loose, saturated or has other
286 unstable characteristics, there is a close relationship between the variation area of earth
287 pressure and the instability range of strata. The definition of n_{sx} is a proportion of the
288 vertical soil pressure box's soil pressure value under various L to its original value. The
289 change law of n_{sx} along and perpendicular to tunnel direction are shown in Figs. 27–29.
290 The n_{sx} in the change range is always less than 1 and progressively gets smaller as L
291 increases under the same burial depth condition. And the closer the earth pressure box
292 is to the excavation face, the smaller the n_{sx} is. In the meantime, the variation area of
293 earth pressure under the same L progressively expands as the buried depth drops, and
294 the n_{sx} at the same place in the variation area gradually decreases. This demonstrates
295 how lowering the burial depth will raise the variation area and disturbed degree of earth
296 pressure, which will in turn raise the range and degree of instability of the strata. In

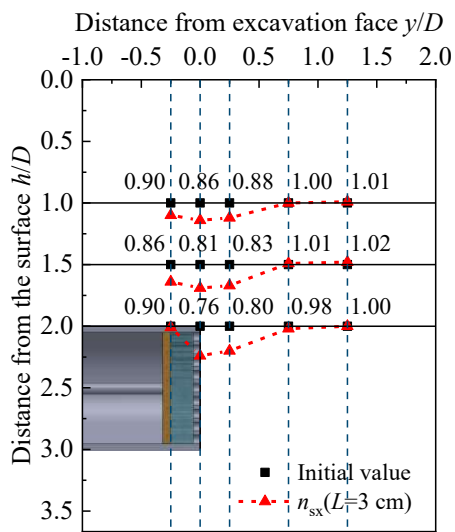
297 addition, when L is equal, the n_{sx} in front of the excavated face is less than the n_{sx}
 298 behind it. The degree of instability in front of the excavation face is higher than that
 299 behind it, as demonstrated by this.



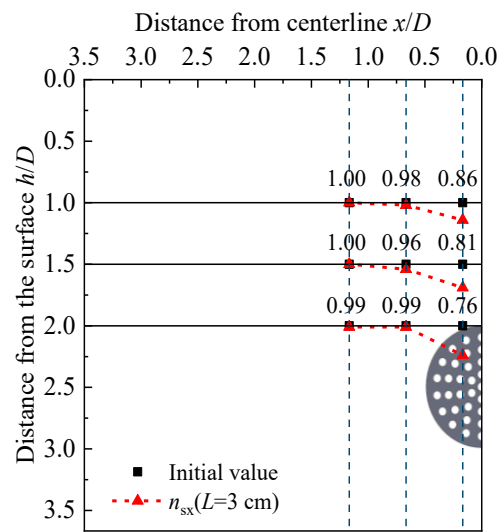
(a) n_{sx} along tunnel for $L = 1.5$ cm



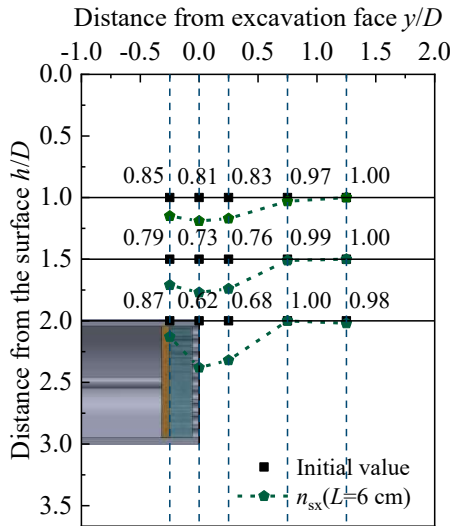
(b) n_{sx} perpendicular to tunnel for $L = 1.5$ cm



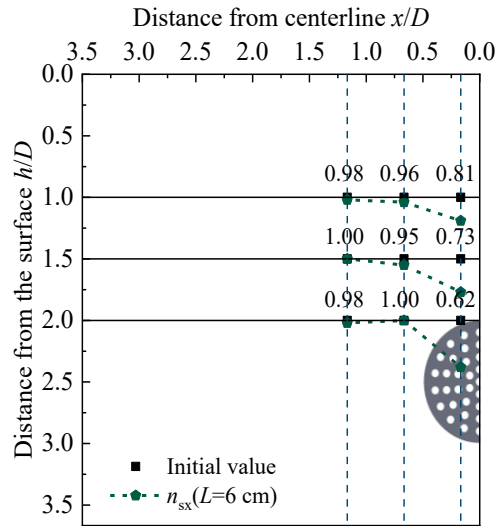
(c) n_{sx} along tunnel for $L = 3$ cm



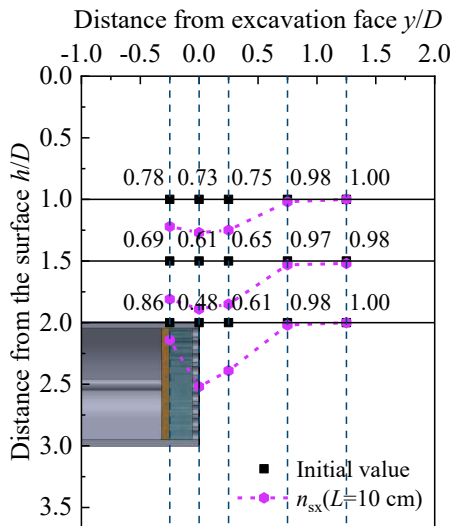
(d) n_{sx} perpendicular to tunnel for $L = 3$ cm



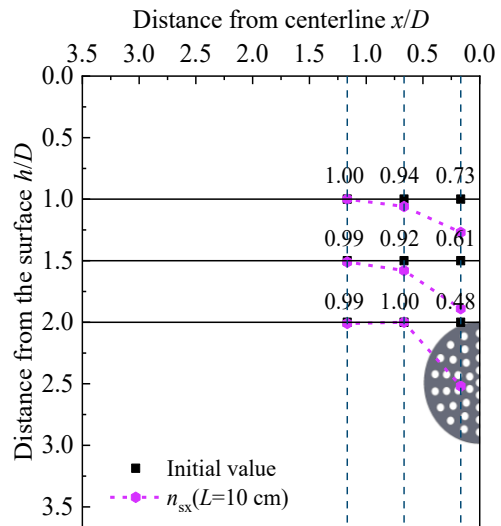
(e) n_{sx} along tunnel for $L = 6$ cm



(f) n_{sx} perpendicular to tunnel for $L = 6$ cm

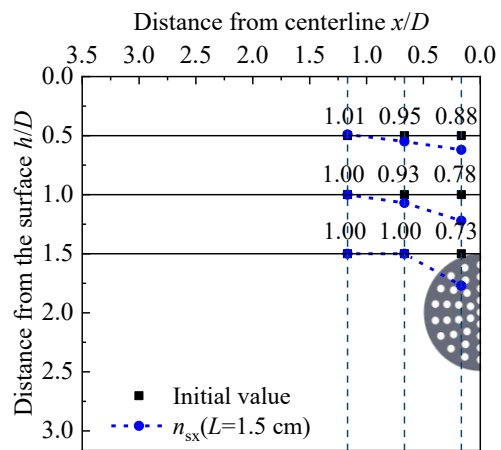
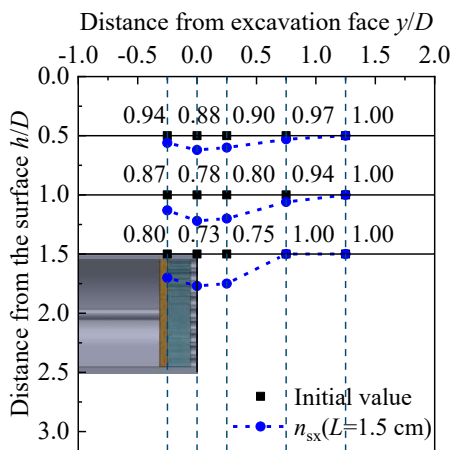


(g) n_{sx} along tunnel for $L = 10$ cm



(h) n_{sx} perpendicular to tunnel for $L = 10$ cm

Fig. 27. The change law of n_{sx} with L for $H/D = 2$.



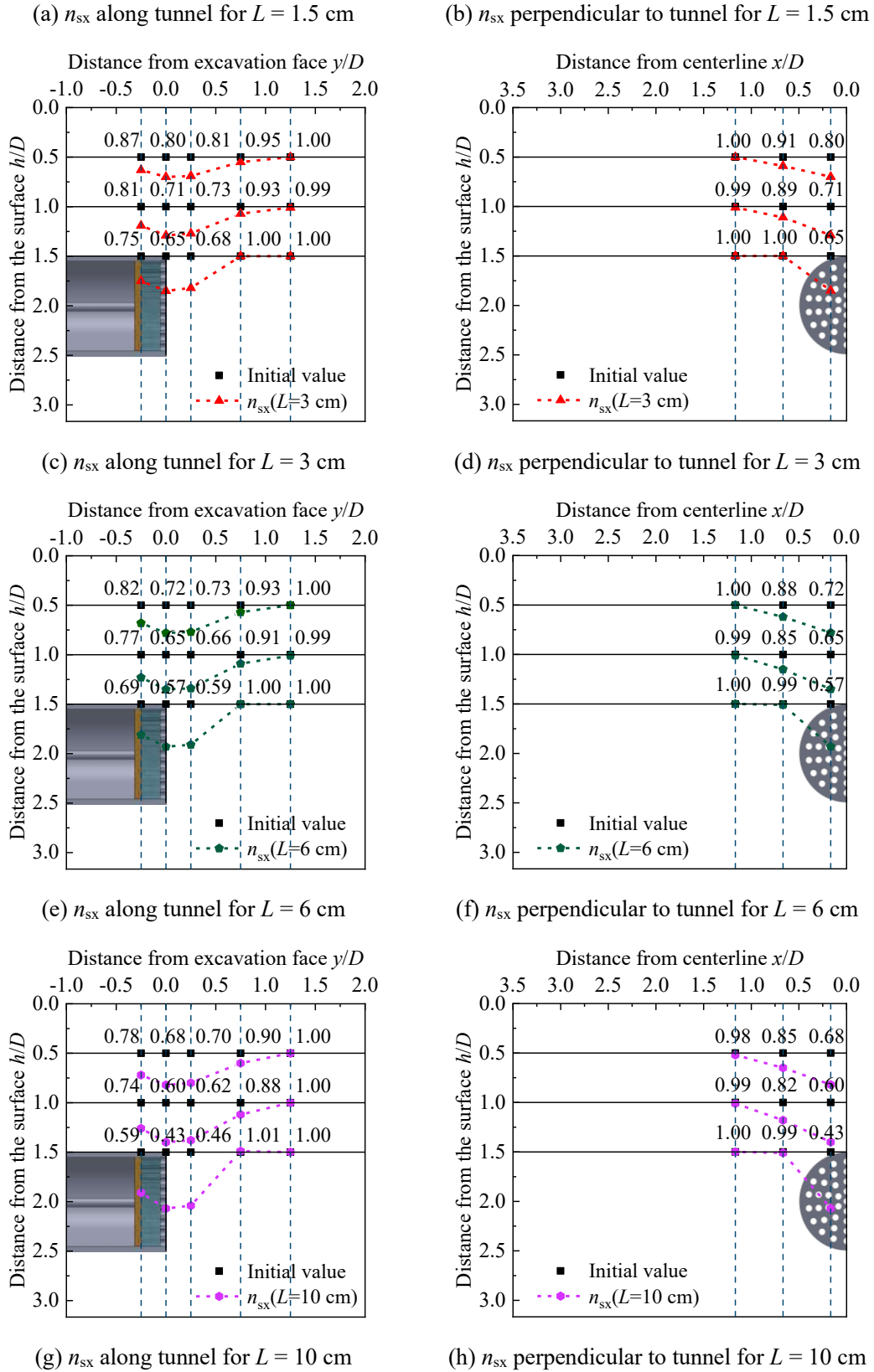
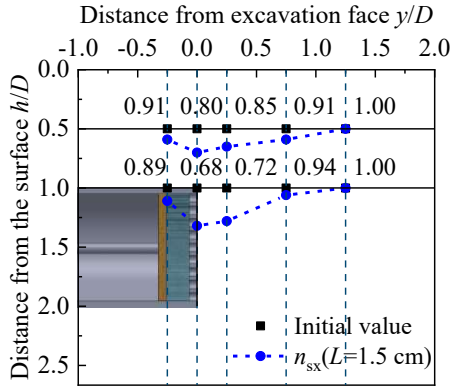
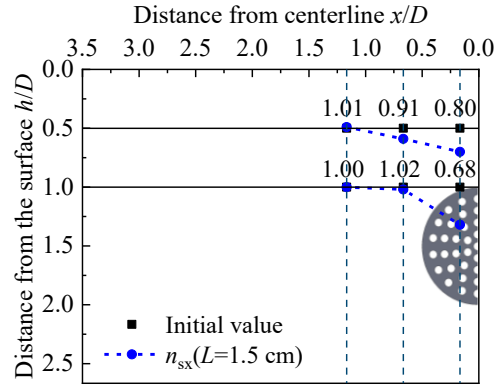


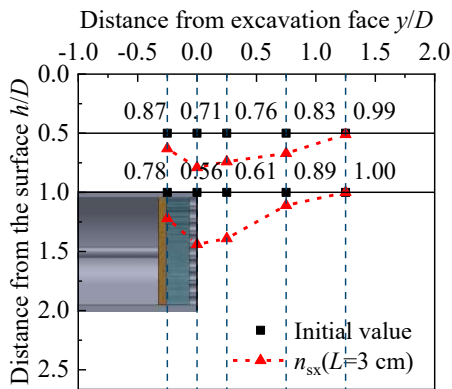
Fig. 28. The change law of n_{sx} with L for $H/D = 1.5$.



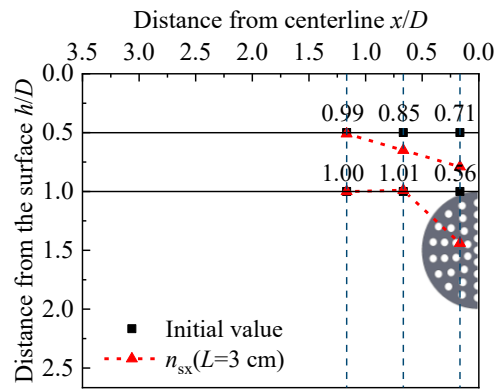
(a) n_{sx} along tunnel for $L = 1.5$ cm



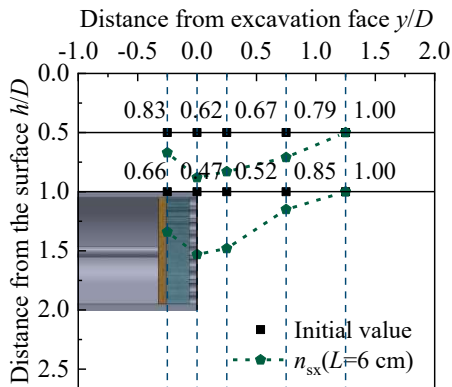
(b) n_{sx} perpendicular to tunnel for $L = 1.5$ cm



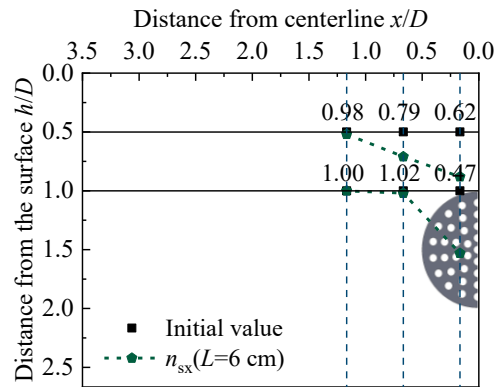
(c) n_{sx} along tunnel for $L = 3$ cm



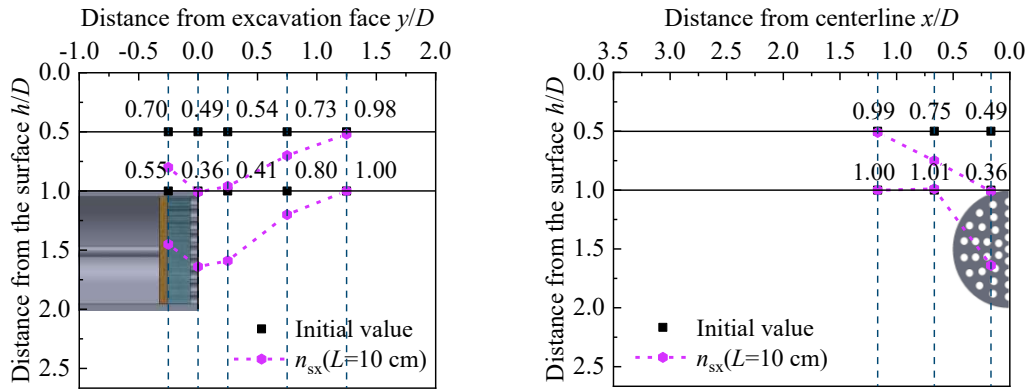
(d) n_{sx} perpendicular to tunnel for $L = 3$ cm



(e) n_{sx} along tunnel for $L = 6$ cm



(f) n_{sx} perpendicular to tunnel for $L = 6$ cm



(g) n_{sx} along tunnel for $L = 10$ cm

(h) n_{sx} perpendicular to tunnel for $L = 10$ cm

Fig. 29. The change law of n_{sx} with L for $H/D = 1$.

302 Under different burial depth conditions, the displacement increment field obtained
 303 by DIC is also the instability range of the strata, as shown in Figs. 30–32. It can be seen
 304 that in the strata with lower dense and upper loose, the instability failure is distributed
 305 in the middle-upper part of the excavation face. The loose stratum in the higher part
 306 primarily controls the strata's deformation and collapse, while the dense sandy pebble
 307 layer maintains its stability. At the same time, as L rises under various burial depths, the
 308 strata's unstable area grows. When the baffle begins to move backwards, the soil arch
 309 forms and gradually develops. If the unstable area is abstracted into geometry, and the
 310 unstable area of the stratum is the model of "quarter ellipsoid + circular table + half
 311 ellipsoid" in this phase. The "quarter ellipsoid + double circular table" model of
 312 excavation face instability is created when the soil arch effect fails, resulting in general
 313 stratum unstable.

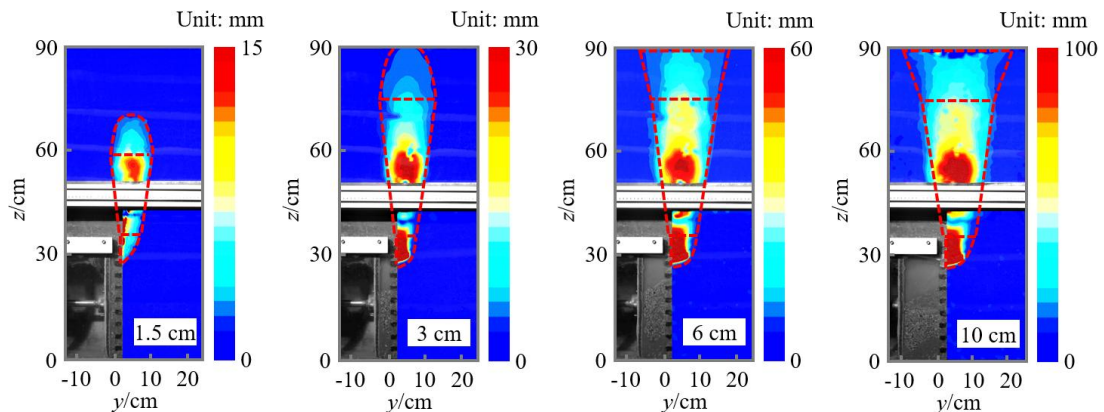


Fig. 30. The change law of instability range with L for $H/D = 2$.

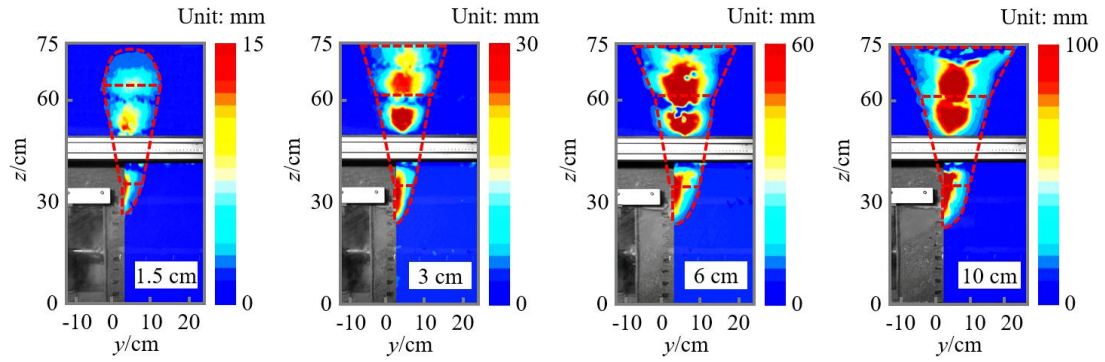


Fig. 31. The change law of instability range with L for $H/D = 1.5$.

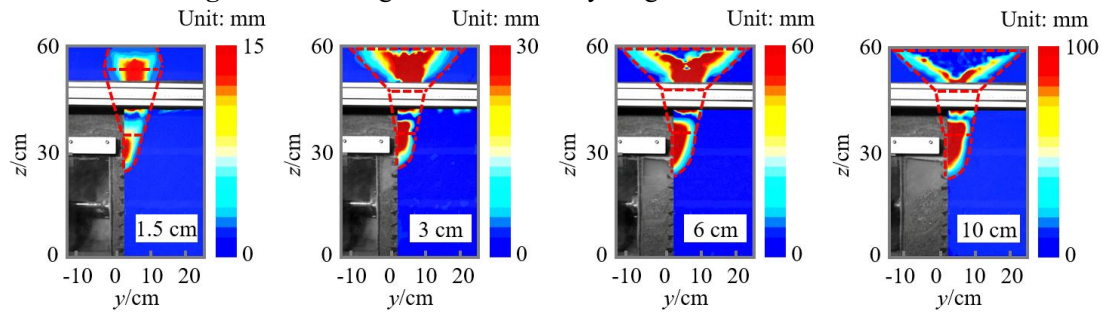
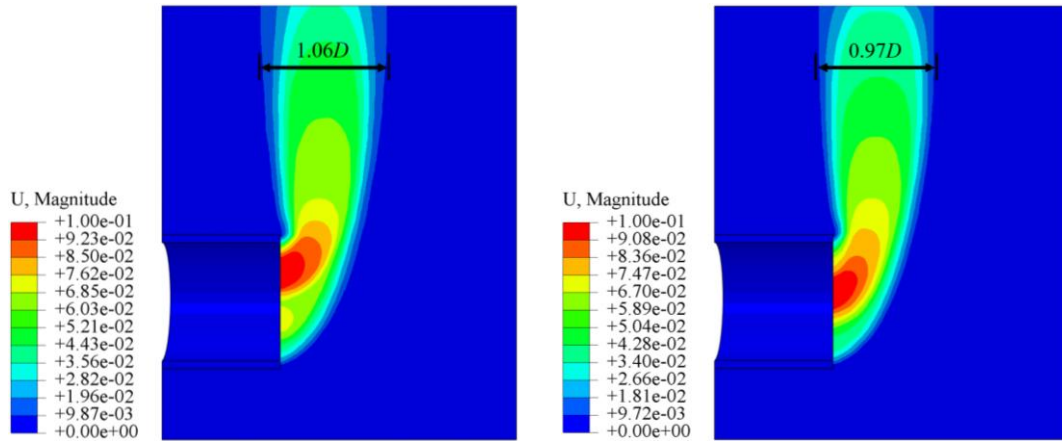


Fig. 32. The change law of instability range with L for $H/D = 1$.

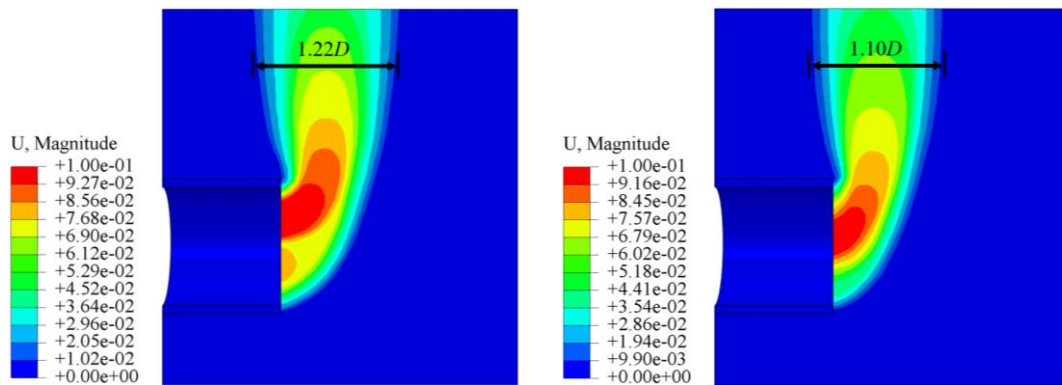
314 In order to further analyze the characteristics of this strata, numerical simulations
 315 are used to compare it with the homogeneous medium dense sandy pebble strata whose
 316 relative compactness D_r is 0.55. The unstable range of the two layers under various
 317 burial depths, as determined by numerical simulations, is displayed in Figs. 33–35 when
 318 $L = 10$ cm. According to the results of model studies, the upper portion of the region
 319 exhibits the greatest displacement of the excavation face in the upper loose and lower
 320 compact layers. However, the maximum displacement of the excavation face in the
 321 homogeneous sandy pebble strata occurs in the middle region. Because the upper
 322 stratum in the lower dense and upper loose stratum is loose and has a low shear strength,
 323 the upper portion of the excavated face destabilizes more readily. The unstable area of
 324 the lower dense and upper loose stratum, which are $1.06D$, $1.22D$, and $1.29D$,
 325 respectively, is shown to progressively rise as the buried depth decreases. And the
 326 unstable area of the uniform stratum whose D_r is 0.55 also increased gradually, which
 327 are $0.97D$, $1.10D$ and $1.20D$, respectively. Lower dense and upper loose strata have a
 328 wider range of unstable than uniform stratum in identical circumstances. This is due to
 329 the discontinuity of stress transfer between loose stratum and dense stratum. When the
 330 loose stratum is unstable, the shear failure will develop along the interface, which
 331 intensifies the growth of the unstable area.



(a) The loose and lower dense strata

(b) The homogeneous strata

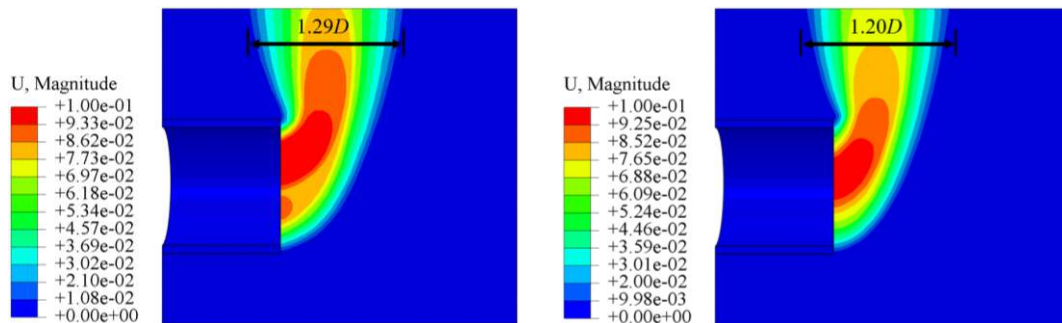
Fig. 33. Comparison of instability range of two strata for $H/D = 2$.



(a) The loose and lower dense strata

(b) The homogeneous strata

Fig. 34. Comparison of instability range of two strata for $H/D = 1.5$.



(a) The loose and lower dense strata

(b) The homogeneous strata

Fig. 35. Comparison of instability range of two strata for $H/D = 1$.

332 **5 Theoretical analysis of excavation face stability**

333 **5.1 Theoretical calculation model of excavation face stability**

334 Combined with the formation instability range obtained in Figs. 30–32, the
 335 theoretical calculation model of excavation face stability is proposed, as shown in Fig.
 336 36. In the calculation model, the soil failure zone in front of excavation is composed of
 337 circular table I, circular table II and wedge III. The distinction between medium-density

338 and slightly-density sandy pebbles marks the division between circular tables I and II.
 339 The boundary between circular table II and wedge III is the dividing line between
 340 medium-density and slightly-density sandy pebbles.

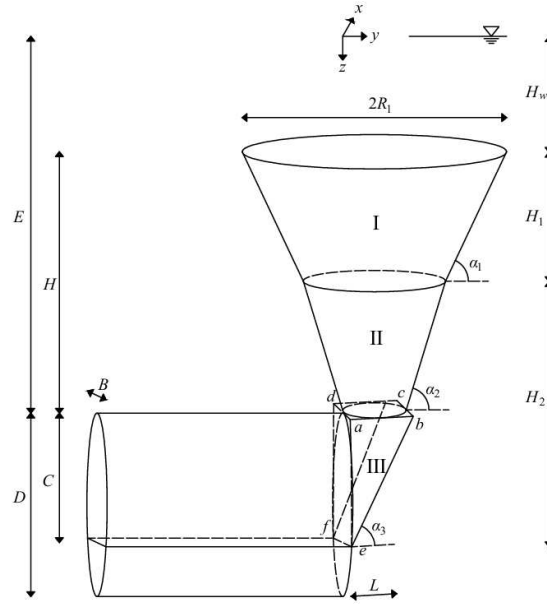


Fig. 36. Theoretical calculation model of excavation face stability.

341 Fig. 36 shows the tunnel's diameter (D), water level height above the tunnel top
 342 (E), and distance between the surface and the tunnel top (H). H_1 is the depth of slightly-
 343 density sandy pebble strata, H_2 is the depth of medium-density sandy pebble formation,
 344 and H_w is the distance of water level above surface. α_1 is the inclination angle of circular
 345 table I, $\alpha_1 = 45^\circ + \frac{\varphi_1}{2}$, and φ_1 is the internal friction angle of slightly dense sandy pebbles.
 346 α_2 is the inclination angle of circular table II. α_3 is the angle between sliding surface of
 347 wedge III and horizontal direction, $\alpha_3 = 45^\circ + \frac{\varphi_2}{2}$, and φ_2 is the internal friction angle
 348 of medium dense sandy pebbles. Points a, b, c, d, e and f are the vertices of wedge III
 349 respectively. Wedge III's width, height, and length are denoted by B, C , and L ,
 350 respectively.

351 The length L of wedge III is:

352
$$L = \frac{C}{\tan \alpha_3} \quad (1)$$

353 According to Terzaghi loose earth pressure theory, the surface will form a loose
 354 zone with the width of $2R_1$, and the upper base radius R_1 of circular table I is:

355
$$R_1 = \frac{D}{2} \cot \left(\frac{\pi}{8} + \frac{\varphi}{4} \right) \quad (2)$$

356 φ is the weighting internal friction angle of strata, which is obtained by Eq. (3).

357
$$\varphi = \frac{\varphi_1 H_1 + \varphi_2 H_2}{H_1 + H_2} \quad (3)$$

358 Since this paper focuses on effective earth pressure, the total earth pressure
 359 brought on by soil weight is the excavation face's limit effective support pressure and
 360 the seepage force (Liu et al. 2016) obtained through numerical simulation that the
 361 seepage direction in the upper soil is basically vertical, while the seepage direction in
 362 the lower wedge is horizontal. So only vertical seepage force is considered when
 363 calculating the upper loose earth pressure, and only horizontal seepage force is
 364 considered when calculating the limit effective support pressure. Under different burial
 365 depths, it can be seen from Figs. 22–24 that the water pressure distribution in the strata
 366 is basically same. In the numerical simulations, the seepage gradient along tunnel
 367 symmetry plane is the largest. The function of vertical and horizontal water pressure on
 368 a symmetric plane is applied to approximate the seepage field distribution in order to
 369 guarantee the safe limit effective support pressure. Fig. 37 displays the relationship
 370 curve between normalized vertical water pressure and tunnel location.

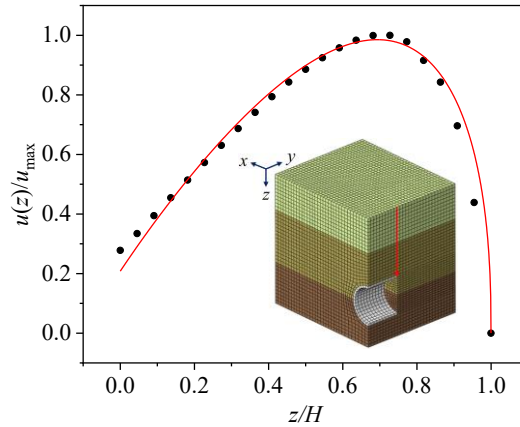


Fig. 37. Normalized $u(z)/u_{\max}$ and z/H relationship curve.

371 Here, z is the depth of the strata, $u(z)$ is the water pressure at the depth from the
 372 surface, and u_{\max} is the maximum of water pressure.

373 Through dimensional analysis and fitting method, $u(z)$ can be obtained by Eq. (4).

374
$$u(z) = \gamma_w E \left(\frac{z - H + E}{E} \right)^{0.92} \left(\frac{H}{D} \right)^{0.44} \sin \left(\frac{1-z}{E} \right)^{0.43} \quad (4)$$

375 The fit degree in the equation is $R^2 = 0.998$.

376 The relationship curve between the normalized water head value and the distance

377 from the excavated face is displayed in Fig. 38 on the central axis in front of the
 378 excavated face.

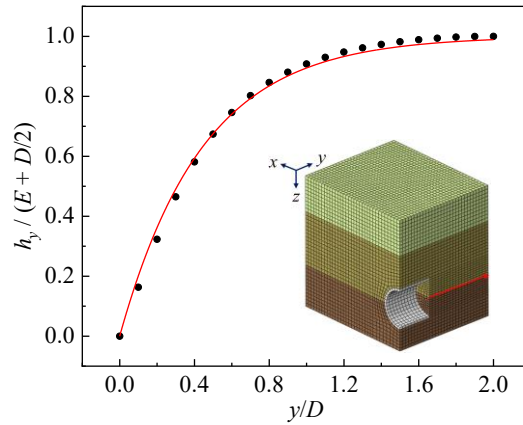


Fig. 38. Normalized $h_y/(E+D/2)$ and y/D relationship curve.

379 Here, h_y is the water head value at position y in wedge III, and y is the distance
 380 between a specific position ahead of the tunnel and the excavated face.

381 Through dimensional analysis and fitting method, h_y can be obtained by Eq. (5).

$$382 \quad h_y = \left(E + \frac{D}{2} \right) \left(1 - e^{-\frac{0.68y}{D}} \right) \quad (5)$$

383 The fit degree in the equation is $R^2 = 0.996$.

384 5.2 Analytical formula of the limit effective support pressure

385 The calculation model of circular table I is shown in Fig. 39.

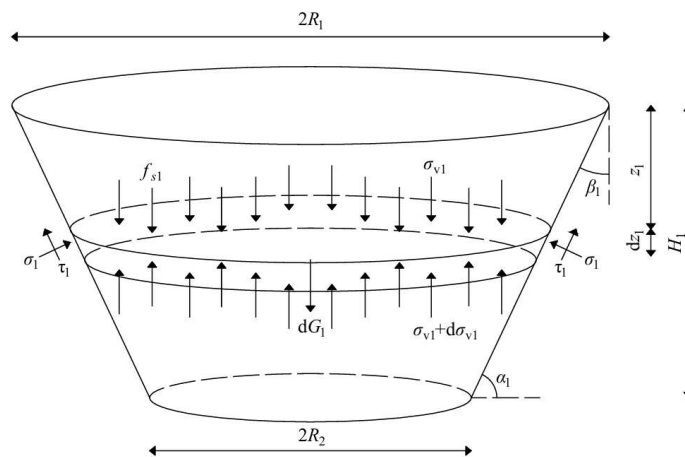


Fig. 39. Circular table I calculation model.

386 In the circular table I, the bottom base radius R_2 is:

$$387 \quad R_2 = R_1 - \frac{H_1}{\tan \alpha_1} \quad (6)$$

388 The angle β_1 between the side and the vertical direction is:

389
$$\beta_1 = 90^\circ - \alpha_1 \quad (7)$$

390 The thickness of micro-body is dz_1 , and the distance z_1 from the upper surface of
391 micro-body to the surface is:

392
$$z_1 = z - H_w \quad (8)$$

393 The area S_1 of the upper surface of micro-body is:

394
$$S_1 = \pi(R_1 - z_1 \tan \beta_1)^2 \quad (9)$$

395 The circumference C_1 of the upper surface of micro-body is:

396
$$C_1 = 2\pi(R_1 - z_1 \tan \beta_1) \quad (10)$$

397 The saturated unit weight of the slightly-density sandy pebble strata is γ_1 , and the
398 gravity dG_1 of micro-body is:

399
$$dG_1 = \gamma_1 \pi (R_1 - z_1 \tan \beta_1)^2 dz_1 \quad (11)$$

400 The effective lateral pressure coefficient k_1 is:

401
$$k_1 = 1 - \sin \varphi_1 \quad (12)$$

402 The relation coefficient K_1 between normal stress on the side and vertical stress is:

403
$$K_1 = k_1 \sin^2 \alpha_1 + \cos^2 \alpha_1 \quad (13)$$

404 The vertical effective compressive stress is σ_{v1} , and the uniform distributed
405 seepage force at height z_1 is f_{s1} . The normal stress σ_1 on the side is:

406
$$\sigma_1 = K_1 \sigma_{v1} \quad (14)$$

407 The tangential stress τ_1 on the side is:

408
$$\tau_1 = K_1 \sigma_{v1} \tan \varphi_1 \quad (15)$$

409 The force balance equation of the micro-body in the vertical direction is as follows:

410
$$\sigma_{v1} S_1 + dG_1 = (\sigma_{v1} + d\sigma_{v1}) S_1 + \tau_1 C_1 \cos \beta_1 dz_1 + \sigma_1 C_1 \sin \beta_1 dz_1 + f_{s1} S_1 \quad (16)$$

411 When $z_1 = 0$, $\sigma_{v1} = 0$. The Eq. (17) is obtained by bringing this boundary condition
412 into the Eq. (16).

413
$$\sigma_{v1} = \frac{\gamma_1 (R_1 - z_1 \tan \beta_1)}{A_1} \left(1 - e^{\frac{-A_1 z_1}{R_1 - z_1 \tan \beta_1}} \right) + 2(E - H) \gamma_w e^{\frac{-A_1 z_1}{R_1 - z_1 \tan \beta_1}}$$

414
$$+ \frac{A_1}{R_1 - z_1 \tan \beta_1} \int_0^{H_1} u(z) e^{\frac{A_1 z_1}{R_1 - z_1 \tan \beta_1}} dz_1 e^{\frac{-A_1 z_1}{R_1 - z_1 \tan \beta_1}}$$

415 (17)

414 Here, $A_1 = 2K_1 (\tan \varphi_1 \cos \beta_1 + \sin \beta_1)$. In Eq. (17), the former one is the loose earth
 415 pressure without considering the seepage, and the latter two are the increase terms
 416 caused by the seepage force.

417 Then the vertical stress q_1 of circular table I acting on circular table II is:

418
$$q_1 = \frac{\gamma_1 R_2}{A_1} \left(1 - e^{\frac{-A_1 H_1}{R_2}} \right) + 2\gamma_w H_w e^{\frac{-A_1 H_1}{R_2}} + \frac{A_1}{R_2} \int_0^{H_1} u(z) e^{\frac{A_1 z_1}{R_1 - z_1 \tan \beta_1}} dz_1 e^{\frac{-A_1 H_1}{R_2}}$$

419 (18)

419 The calculation model of circular table II is shown in Fig. 40.

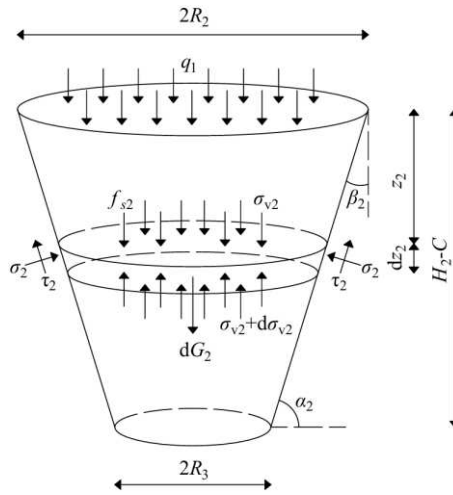


Fig. 40. Circular table II calculation model.

420 Based on the area equivalency principle, the bottom base radius R_3 in the circular table
 421 II is:

422
$$R_3 = \sqrt{\frac{BL}{\pi}}$$

423 (19)

423 The inclination angle α_2 of circular table is:

424
$$\alpha_2 = \arctan \frac{H_2 - C}{R_2 - R_3}$$

425 (20)

425 The angle β_2 between the side and the vertical direction is:

426
$$\beta_2 = 90^\circ - \alpha_2$$

427 (21)

427 The thickness of micro-body is dz_2 , and the distance z_2 from the upper surface of
 428 micro-body to the surface is:

$$429 \quad z_2 = z - H_w - H_1 \quad (22)$$

430 The effective lateral pressure coefficient k_2 is:

$$431 \quad k_2 = 1 - \sin \varphi_2 \quad (23)$$

432 The relation coefficient K_2 between normal stress on the side and vertical stress is:

$$433 \quad K_2 = k_2 \sin^2 \alpha_2 + \cos^2 \alpha_2 \quad (24)$$

434 Similarly, according to the analysis steps of circular table I, the force analysis of
 435 the micro-body in circular table II is carried out.

436 The vertical stress q_2 of circular table II acting on wedge III is:

$$437 \quad q_2 = \frac{\gamma_2 R_3}{A_2} \left[1 - e^{\frac{-A_2(H_2-C)}{R_3}} \right] + q_1 e^{\frac{-A_2(H_2-C)}{R_3}} + \frac{A_2}{R_3} \int_0^{H_2-C} u(z) e^{\frac{A_2 z_2}{R_2 - z_2 \tan \beta_2}} dz_2 e^{\frac{-A_2(H_2-C)}{R_3}} \quad (25)$$

438 Here, $A_2 = 2K_2 (\tan \varphi_2 \cos \beta_2 + \sin \beta_2)$.

439 The calculation model of wedge III is shown in Fig. 41.

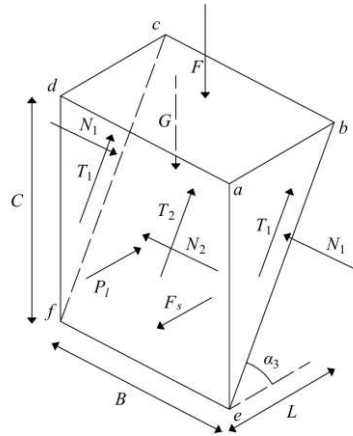


Fig. 41. Wedge III calculation model.

440 In Fig. 41, the force F of circular table II acting on wedge III is:

$$441 \quad F = q_2 S_3 \quad (26)$$

442 Here, the bottom area of circular table II is S_3 , and $S_3 = \pi R_3^2$.

443 The hydraulic gradient is obtained by Eq. (5) and integrated in wedge III. The
 444 horizontal seepage force F_s is:

445
$$F_s = -\gamma_w \left[0.39L + \frac{0.68EL}{D} \right] \times \int_0^{\frac{L}{\tan \alpha_3}} (L - y \tan \alpha_3) e^{\frac{-0.68y}{D}} dy \quad (27)$$

446 The wedge III's gravity G is:

447
$$G = \frac{1}{2} BCL\gamma_2 \quad (28)$$

448 Here, γ_2 is the saturated unit weight of the medium dense sandy pebble stratum.

449 The friction force T_1 acting on the side of wedge III is:

450
$$T_1 = S_c \tau_c \quad (29)$$

451 Here, the side area of wedge III is S_c , $S_c = \frac{1}{2} CL$. The tangential stress acting on the

452 side of wedge is τ_c , $\tau_c = k_2 \left(q_2 + \frac{\gamma_2 C}{3} \right) \tan \varphi_2$, and $k_2 = 1 - \sin \varphi_2$.

453 On the side of wedge III, the pressure N_1 is:

454
$$N_1 = \frac{T_1}{\tan \varphi_2} \quad (30)$$

455 The relationship between the friction force T_2 and the pressure N_2 acting on the
456 sliding surface of wedge III can be obtained by Eq. (31).

457
$$T_2 = N_2 \tan \varphi_2 \quad (31)$$

458 The force analysis of wedge III is carried out, and the equation for force balance
459 in the horizontal direction is as follows:

460
$$P_l + 2T_1 \cos \alpha_3 + T_2 \cos \alpha_3 = N_2 \sin \alpha_3 + F_s \quad (32)$$

461 In Eq. (32), P_l is the excavation face's maximum effective support pressure.

462 The following is the force balance equation in the vertical direction:

463
$$F + G = 2T_1 \sin \alpha_3 + T_2 \sin \alpha_3 + N_2 \cos \alpha_3 \quad (33)$$

464 The parameters in Eqs. (26) to (31) are substituted into Eqs. (32) to (33), and the
465 limit effective support pressure P_l is:

466
$$P_l = \delta (F + G - 2T_1 \sin \alpha_3) + F_s - 2T_1 \cos \alpha_3 \quad (34)$$

467 Here, $\delta = \frac{\sin \alpha_3 \cot \varphi_2 - \cos \alpha_3}{\sin \alpha_3 + \cos \alpha_3 \cot \varphi_2}$.

468 **5.3 Verification of theoretical calculation results**

469 For the lower dense and upper loose saturated sandy pebble stratum, the excavated
470 face deformation occurs in medium dense sandy pebble stratum. The relationship
471 between the upper loose soil and support force should be the primary focus when
472 evaluating the stability of the excavation face.

473 According to the theoretical computation, the excavation face's limit effective
474 support compressive stress σ_l is:

$$475 \quad \sigma_l = \frac{P_l}{BC} \quad (35)$$

476 Here, $B = D$ and $C = \frac{D}{2}$.

477 The difference between the average water pressure and the average saturated earth
478 pressure on the upper half of the excavation face is represented by σ_l in model tests.
479 The average value of earth pressure boxes No. 1, No. 2, No. 3, and No. 6 is used to
480 calculate the saturated earth pressure. The average reading from the No. 1, No. 2, and
481 No. 5 osmometers is used to calculate the water pressure.

482 Fig. 42 compares the results of model tests with those of theoretical calculations.
483 The limit effective support compressive stress determined by theoretical calculation
484 progressively rises to 1.882 kPa, 2.227 kPa, and 2.431 kPa, respectively, as the buried
485 depth increases. The limit effective support compressive stress obtained by model test
486 also gradually increases to 2.007 kPa, 2.332 kPa and 2.747 kPa, respectively. The
487 findings indicate that as buried depth increases, so does the limit effective support
488 compressive stress. Under the same burial depth condition, model test results are greater
489 than theoretical calculation results. This is because the baffle is subjected to the friction
490 resistance of the circular aluminum cylinder in the test process, resulting in a larger
491 support force on the excavated face. The accuracy of the theoretical calculation model
492 is confirmed by the good agreement between the theoretical calculation results and the
493 model test results, with an error of less than 12%.

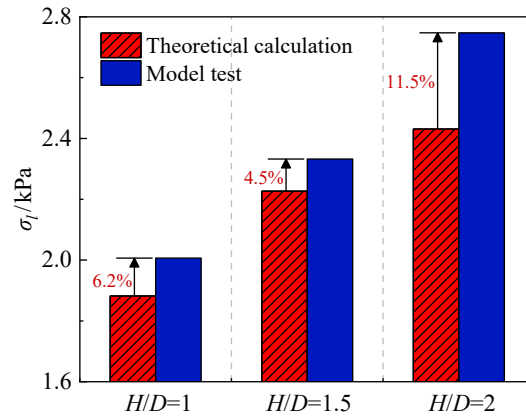


Fig. 42. Comparison of the results of model test and theoretical calculation.

494 6 Conclusions

495 The stability of the excavation face under different buried depths is examined in
 496 this paper using numerical simulations and model tests for the upper loose saturated
 497 sandy pebble strata and lower dense strata. Based on DIC technology, the excavated
 498 face's progressive failure process with active instability is analyzed, and the theoretical
 499 calculation model of excavation face is presented. In the meantime, the analytical
 500 formula of the limit effective support force of the excavated face taking seepage impact
 501 into account is derived, and the fitted seepage force formula is introduced into
 502 theoretical calculation. The main conclusions are as follows.

503 (1) The change process of peak displacement is separated into three stages based
 504 on the change law of highest displacement of ground settlement with L under various
 505 buried depth conditions. There are no settlement stage, slow settlement stage and rapid
 506 settlement stage respectively. With the decrease of the buried depth, there is a gradual
 507 increase in both the magnitude and extent of ground settlement.

508 (2) The water pressure in front of the excavation face shows a trend of first rising
 509 and then stabilizing with the increase of L under various burial depth conditions. The
 510 decrease of buried depth will increase the seepage velocity of water in the strata, while
 511 having no effect on the seepage path range of water.

512 (3) Accordingly, the equivalent L in the limit equilibrium condition is 3.5 cm, 2.5
 513 cm, and 1.9 cm as the buried depth decreases. This result implies that the general
 514 instability of the stratum will occur beforehand as the buried depth decreases.

515 (4) With the decrease of buried depth, the range and degree of strata instability
 516 increase gradually. When the overall instability of the stratum happens, an excavation
 517 face instability model of "quarter ellipsoid + double circular table" is formed. Compared

518 with the homogeneous sandy pebble strata, the instability area of lower dense and upper
519 loose stratum is larger.

520 (5) The theoretical calculation model of excavation face is composed of circular
521 table I, circular table II and wedge III. The excavation face's limit effective support
522 compressive stress rises as the buried depth does.

523 **Data Availability**

524 Data supporting this research article are available from the corresponding author
525 on request.

526 **Declaration of Competing Interest**

527 The authors declare that they have no known competing financial interests or
528 personal relationships that could have appeared to influence the work reported in this
529 paper.

530 **Acknowledgements**

531 The authors would like to respect and thank all reviewers for their constructive
532 and helpful review.

533 **Funding**

534 The authors gratefully acknowledge the financial support provided by the National
535 Natural Science Foundation of China (No. 52278382) and Natural Science Foundation
536 of Beijing Municipality (No. 8222004).

537 **References**

- 538 Alagha ASN, Chapman DN (2019) Numerical modelling of tunnel face stability in homogeneous
539 and layered soft ground. *Tunnelling and Underground Space Technology* 94:103096.
540 <https://doi.org/10.1016/j.tust.2019.103096>
- 541 Antão AN, Vicente Da Silva M, Monteiro N, Deusdado N (2021) Upper and lower bounds for three-
542 dimensional undrained stability of shallow tunnels. *Transportation Geotechnics* 27:100491.
543 <https://doi.org/10.1016/j.trgeo.2020.100491>
- 544 Mi B, Xiang Y (2020) Model experiment and calculation analysis of excavation-seepage stability
545 for shallow shield tunneling in sandy ground
- 546 Chen R, Yin X, Tang L, Chen Y (2018) Centrifugal model tests on face failure of earth pressure
547 balance shield induced by steady state seepage in saturated sandy silt ground. *Tunnelling and*
548 *Underground Space Technology* 81:315–325. <https://doi.org/10.1016/j.tust.2018.06.031>
- 549 Chen X, Hu Y, Yao K, Leal Sousa R (2024) Large-deformation finite-element modelling of face
550 instability during tunnelling in clayey soils: Incorporating dynamic excavation process.
551 *Tunnelling and Underground Space Technology* 153:106038.
552 <https://doi.org/10.1016/j.tust.2024.106038>
- 553 Cheng C, Jia P, Ni P, et al (2023a) Upper bound analysis of longitudinally inclined EPB shield tunnel

554 face stability in dense sand strata. *Transportation Geotechnics* 41:101031.
555 <https://doi.org/10.1016/j.trgeo.2023.101031>

556 Cheng C, Yang H, Jia P, et al (2023b) Face stability of shallowly buried large-section EPB box
557 jacking crossing the Beijing-Hangzhou Grand Canal. *Tunnelling and Underground Space*
558 *Technology* 138:105200. <https://doi.org/10.1016/j.tust.2023.105200>

559 Cui X, Li P, Chen Y, et al (2025a) Analysis of face stability for a shield tunnel in the inclined strata
560 with soft upper and hard lower layers. *Alexandria Engineering Journal* 125:677–691.
561 <https://doi.org/10.1016/j.aej.2025.04.013>

562 Cui X, Li P, Ge Z, et al (2025b) Experimental study on face stability of shield tunnel in water-rich
563 inclined composite strata considering different inclination angles. *Applied Ocean Research*
564 154:104323. <https://doi.org/10.1016/j.apor.2024.104323>

565 Cui X, Li P, Wang C, et al (2025c) Effect of seepage flow on face stability for a tunnel in water-rich
566 silty clay overlying sandy cobble strata. *Tunnelling and Underground Space Technology*
567 161:106539. <https://doi.org/10.1016/j.tust.2025.106539>

568 Cui X, Li P, Wu J, Wei Y (2024) Stability Analysis of a Shield Tunnel in Unsaturated Soil
569 Considering the Soil Arch Effect. *Int J Geomech* 24:04024041.
570 <https://doi.org/10.1061/IJGNALGMENG-8709>

571 Di Q, Li P, Zhang M, et al (2022) Analysis of face stability for tunnels under seepage flow in the
572 saturated ground. *Ocean Engineering* 266:112674.
573 <https://doi.org/10.1016/j.oceaneng.2022.112674>

574 Di Q, Li P, Zhang M, et al (2024) Experimental study on the effect of seepage flow on the tunnel
575 face stability in the saturated ground. *Ocean Engineering* 299:117074.
576 <https://doi.org/10.1016/j.oceaneng.2024.117074>

577 Di Q, Li P, Zhang M, Cui X (2023) Experimental investigation of face instability for tunnels in
578 sandy cobble strata. *Underground Space* 10:199–216.
579 <https://doi.org/10.1016/j.undsp.2022.10.004>

580 Ding W, Liu K, Shi P, et al (2019) Face stability analysis of shallow circular tunnels driven by a
581 pressurized shield in purely cohesive soils under undrained conditions. *Computers and*
582 *Geotechnics* 107:110–127. <https://doi.org/10.1016/j.compgeo.2018.11.025>

583 Ding X, Li K, Xie Y, Liu S (2022) Face stability analysis of large shield-driven tunnel in rock-soil
584 interface composite formations. *Underground Space* 7:1021–1035.
585 <https://doi.org/10.1016/j.undsp.2022.01.007>

586 Fu Y, Zeng D, Xiong H, et al (2022) Seepage effect on failure mechanisms of the underwater tunnel
587 face via CFD–DEM coupling. *Computers and Geotechnics* 146:104591.
588 <https://doi.org/10.1016/j.compgeo.2021.104591>

589 Ge C, Yang M, Li P, et al (2024) Performance and environmental impacts of deep foundation
590 excavation in soft soils: A field and modeling-based case study in Nanjing, China. *Underground*
591 *Space* 18:218–238. <https://doi.org/10.1016/j.undsp.2024.01.002>

592 Habumuremyi P, Xiang Y (2023) A 3-D analytical continuous upper bound limit analysis for face
593 stability of shallow shield tunneling in undrained clays. *Computers and Geotechnics*
594 164:105779. <https://doi.org/10.1016/j.compgeo.2023.105779>

595 Han K, Wang L, Su D, et al (2021) An analytical model for face stability of tunnels traversing the

596 fault fracture zone with high hydraulic pressure. *Computers and Geotechnics* 140:104467.
597 <https://doi.org/10.1016/j.compegeo.2021.104467>

598 Hou CT, Yang XL (2022) 3D stability analysis of tunnel face with influence of unsaturated transient
599 flow. *Tunnelling and Underground Space Technology* 123:104414.
600 <https://doi.org/10.1016/j.tust.2022.104414>

601 Hu X, Fu W, Woody Ju J, et al (2021) Face stability conditions in granular soils during the advancing
602 and stopping of earth-pressure-balanced-shield machine. *Tunnelling and Underground Space*
603 *Technology* 109:103755. <https://doi.org/10.1016/j.tust.2020.103755>

604 Jia Z, Bai Y, Liu C, et al (2023) Visualization investigation on stability of shield tunnel face with
605 transparent soil, considering different longitudinal inclination angles. *Tunnelling and*
606 *Underground Space Technology* 137:105154. <https://doi.org/10.1016/j.tust.2023.105154>

607 Kong D, Teng S, Shi J, Zhao M (2024) An Improved Failure Model Considering the Arching Effect
608 for Tunnel Face Stability in a Weak and Fractured Rock Mass. *Int J Geomech* 24:04024094.
609 <https://doi.org/10.1061/IJGNALGMENG-9028>

610 Lei H, Xu Y, Liu M, Zhong H (2024) Face Stability Analysis of Shield Tunnel in Cohesive–
611 Frictional Soils Considering Soil Arch Evolution. *Int J Geomech* 24:04024275.
612 <https://doi.org/10.1061/IJGNALGMENG-9391>

613 Li P, Cui X, Xia J, Wang X (2023) Analytical solutions of limit support pressure and vertical earth
614 pressure on cutting face for tunnels. *Underground Space* 12:65–78.
615 <https://doi.org/10.1016/j.undsp.2023.02.004>

616 Li P, Wang C, Cui X, et al (2025) Experimental investigation on the stability of shield tunnel
617 excavation face in upper loose and lower dense water-rich strata. *J Zhejiang Univ Sci A*
618 26:471–491. <https://doi.org/10.1631/jzus.A2400309>

619 Li W, Zhang C, Tan Z, Ma M (2021) Effect of the seepage flow on the face stability of a shield
620 tunnel. *Tunnelling and Underground Space Technology* 112:103900.
621 <https://doi.org/10.1016/j.tust.2021.103900>

622 Lin Q, Lu D, Lei C, et al (2021) Model test study on the stability of cobble strata during shield
623 under-crossing. *Tunnelling and Underground Space Technology* 110:103807.
624 <https://doi.org/10.1016/j.tust.2020.103807>

625 Liu Q, Liu Z, Xue Y, et al (2024) Deformation features and failure mechanism of subsea shield
626 tunnels with different burial depths crossing fault-zone. *Marine Georesources &*
627 *Geotechnology* 42:679–693. <https://doi.org/10.1080/1064119X.2023.2214132>

628 Liu W, Albers B, Zhao Y, Tang X (2016) Upper bound analysis for estimation of the influence of
629 seepage on tunnel face stability in layered soils. *J Zhejiang Univ Sci A* 17:886–902.
630 <https://doi.org/10.1631/jzus.A1500233>

631 Liu X, Wang F, Fang H, Yuan D (2019) Dual-failure-mechanism model for face stability analysis of
632 shield tunneling in sands. *Tunnelling and Underground Space Technology* 85:196–208.
633 <https://doi.org/10.1016/j.tust.2018.12.003>

634 Lu X, Zhou Y, Huang M, Li F (2017) Computation of the Minimum Limit Support Pressure for the
635 Shield Tunnel Face Stability Under Seepage Condition. *Int J Civ Eng* 15:849–863.
636 <https://doi.org/10.1007/s40999-016-0116-0>

637 Lü X, Zhou Y, Huang M, Zeng S (2018) Experimental study of the face stability of shield tunnel in

638 sands under seepage condition. *Tunnelling and Underground Space Technology* 74:195–205.
639 <https://doi.org/10.1016/j.tust.2018.01.015>

640 Ma S, Duan Z, Huang Z, et al (2022a) Study on the stability of shield tunnel face in clay and clay-
641 gravel stratum through large-scale physical model tests with transparent soil. *Tunnelling and*
642 *Underground Space Technology* 119:104199. <https://doi.org/10.1016/j.tust.2021.104199>

643 Ma S, Li J, Li Z (2022b) Critical support pressure of shield tunnel face in soft-hard mixed strata.
644 *Transportation Geotechnics* 37:100853. <https://doi.org/10.1016/j.trgeo.2022.100853>

645 Tu S, Li W, Zhang C, et al (2024) Model test and discrete element method simulation of tunnel face
646 stability in sand-gravel inclined layered stratum. *Computers and Geotechnics* 172:106456.
647 <https://doi.org/10.1016/j.compgeo.2024.106456>

648 Wang C, Hou J, Ye X-W, et al (2023a) A 3D torus-slice model for limit equilibrium analysis of
649 shield tunnel face under soil arching effect. *Engineering Failure Analysis* 146:107148.
650 <https://doi.org/10.1016/j.engfailanal.2023.107148>

651 Wang F, Du X, Li P (2023b) Predictions of ground surface settlement for shield tunnels in sandy
652 cobble stratum based on stochastic medium theory and empirical formulas. *Underground Space*
653 11:189–203. <https://doi.org/10.1016/j.undsp.2023.01.003>

654 Wang J, Lin G, Xu G, et al (2022) Face stability of EPB shield tunnels in multilayered ground with
655 soft sand lying on hard rock considering dynamic excavation process: A DEM study.
656 *Tunnelling and Underground Space Technology* 120:104268.
657 <https://doi.org/10.1016/j.tust.2021.104268>

658 Wang J, Tian N, Lin G, et al (2024) Face failure of deep EPB shield tunnels in dry graded cobble-
659 rich soil: A DEM study. *Tunnelling and Underground Space Technology* 147:105622.
660 <https://doi.org/10.1016/j.tust.2024.105622>

661 Wang L, Han K, Xie T, Luo J (2019) Calculation of Limit Support Pressure for EPB Shield Tunnel
662 Face in Water-Rich Sand. *Symmetry* 11:1102. <https://doi.org/10.3390/sym11091102>

663 Weng X, Sun Y, Yan B, et al (2020) Centrifuge testing and numerical modeling of tunnel face
664 stability considering longitudinal slope angle and steady state seepage in soft clay. *Tunnelling*
665 *and Underground Space Technology* 101:103406. <https://doi.org/10.1016/j.tust.2020.103406>

666 Wong KS, Ng CWW, Chen YM, Bian XC (2012) Centrifuge and numerical investigation of passive
667 failure of tunnel face in sand. *Tunnelling and Underground Space Technology* 28:297–303.
668 <https://doi.org/10.1016/j.tust.2011.12.004>

669 Yang F, Qin A, Zheng X, et al (2024) Stability and Failure Mechanism of the Tunnel Face in
670 Nonhomogeneous Clay with Longitudinal Slopes: A Kinematic Limit Analysis. *Int J Geomech*
671 24:04024212. <https://doi.org/10.1061/IJGNAI.GMENG-9782>

672 Yang X-L, Zhong J-H (2019) Stability Analysis of Tunnel Face in Nonlinear Soil under Seepage
673 Flow. *KSCE Journal of Civil Engineering* 23:4553–4563. [https://doi.org/10.1007/s12205-019-](https://doi.org/10.1007/s12205-019-0601-5)
674 [0601-5](https://doi.org/10.1007/s12205-019-0601-5)

675 Ye Z, Wu H, Wang C, et al (2022) Limit face pressure analysis of an EPB shield under suffusion
676 conditions. *Tunnelling and Underground Space Technology* 130:104733.
677 <https://doi.org/10.1016/j.tust.2022.104733>

678 Yi C, Senent S, Jimenez R (2019) Effect of advance drainage on tunnel face stability using Limit
679 Analysis and numerical simulations. *Tunnelling and Underground Space Technology*

680 93:103105. <https://doi.org/10.1016/j.tust.2019.103105>

681 Yin X, Chen R, Meng F (2021) Influence of seepage and tunnel face opening on face support
682 pressure of EPB shield. *Computers and Geotechnics* 135:104198.
683 <https://doi.org/10.1016/j.compgeo.2021.104198>

684 Zhang D, Ma Z, Yu B, Yin H (2019) Upper bound solution of surrounding rock pressure of shallow
685 tunnel under nonlinear failure criterion. *J Cent South Univ* 26:1696–1705.
686 <https://doi.org/10.1007/s11771-019-4126-3>

687 Zhang S, Cheng X, Qi L, Zhou X (2022a) Face stability analysis of large diameter shield tunnel in
688 soft clay considering high water pressure seepage. *Ocean Engineering* 253:111283.
689 <https://doi.org/10.1016/j.oceaneng.2022.111283>

690 Zhang Y, Tao L, Zhao X, et al (2022b) An analytical model for face stability of shield tunnel in dry
691 cohesionless soils with different buried depth. *Computers and Geotechnics* 142:104565.
692 <https://doi.org/10.1016/j.compgeo.2021.104565>

693 Zhao Y, Yang Z, Chen Z, Ling D (2024) A Modified Wedge-Prism Model for Calculating the Limit
694 Support Pressure of a Shallow Shield Tunnel Face in Unsaturated Sandy Soil. *Int J Geomech*
695 24:04024233. <https://doi.org/10.1061/IJGNAI.GMENG-10131>

696